

CS 161

Intro to CS I

Recursion

Example: Factorial

- Definition

$$0! = 1;$$

$$n! = n * (n-1) * \dots * (n-(n-1)) * 1 = n * (n-1)! ; n > 0$$

Iterative Factorial

factorial(0) = 1;

factorial(n) = $n * n-1 * n-2 * \dots * n-(n-1) * 1$;

```
long factorial(int n) {  
    long fact;  
    if(n==0)  
        fact=1;  
    else  
        for(fact=n; n > 1; n--)  
            fact=fact*(n-1);  
    return fact;  
}
```

Recursive Factorial

`factorial(0) = 1;`

`factorial(n) = n*factorial(n-1);`

```
long factorial(int n) {  
    if (n == 0)    // Base case  
        return 1;  
    else  
        return n * factorial(n - 1);    // Recursive call  
}
```

Computing Factorial Iteratively

factorial(4)

```
factorial(0) = 1;
```

```
factorial(n) = n*(n-1)*...*2*1;
```

Computing Factorial Iteratively

$$\text{factorial}(4) = 4 * 3$$

```
factorial(0) = 1;
```

```
factorial(n) = n*(n-1)*...*2*1;
```

Computing Factorial Iteratively

$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

Computing Factorial Iteratively

$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2 \\ &= 24 * 1\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```


Computing Factorial Iteratively

$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2 \\ &= 24 * 1 \\ &= 24\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

Computing Factorial Recursively

factorial(4)

```
factorial(0) = 1;  
factorial(n) = n*factorial(n-1);
```

Computing Factorial Recursively

$$\text{factorial}(4) = 4 * \text{factorial}(3)$$

```
factorial(0) = 1;  
factorial(n) = n*factorial(n-1);
```

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1)))\end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \\ &= 4 * 6\end{aligned}$$

Computing Factorial Recursively

```
factorial(0) = 1;
```

```
factorial(n) = n*factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \\ &= 4 * 6 \\ &= 24\end{aligned}$$

Differences

- Pros
 - Readability
- Cons
 - Efficiency
 - Memory

Recursive Factorial

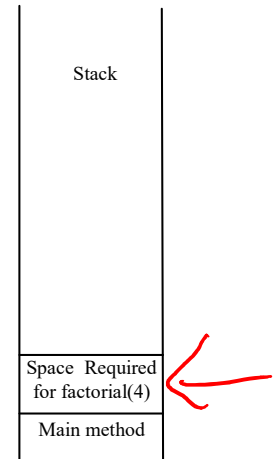
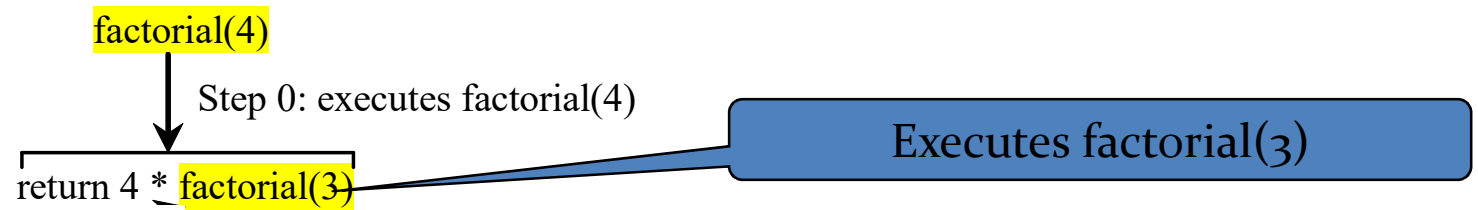
factorial(4)

Executes factorial(4)

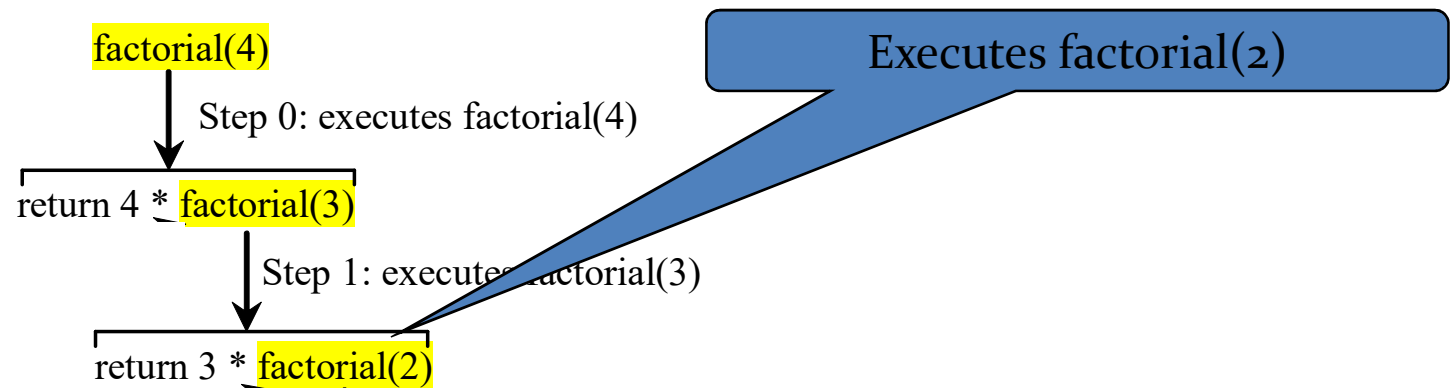
Stack

Main method

Recursive Factorial

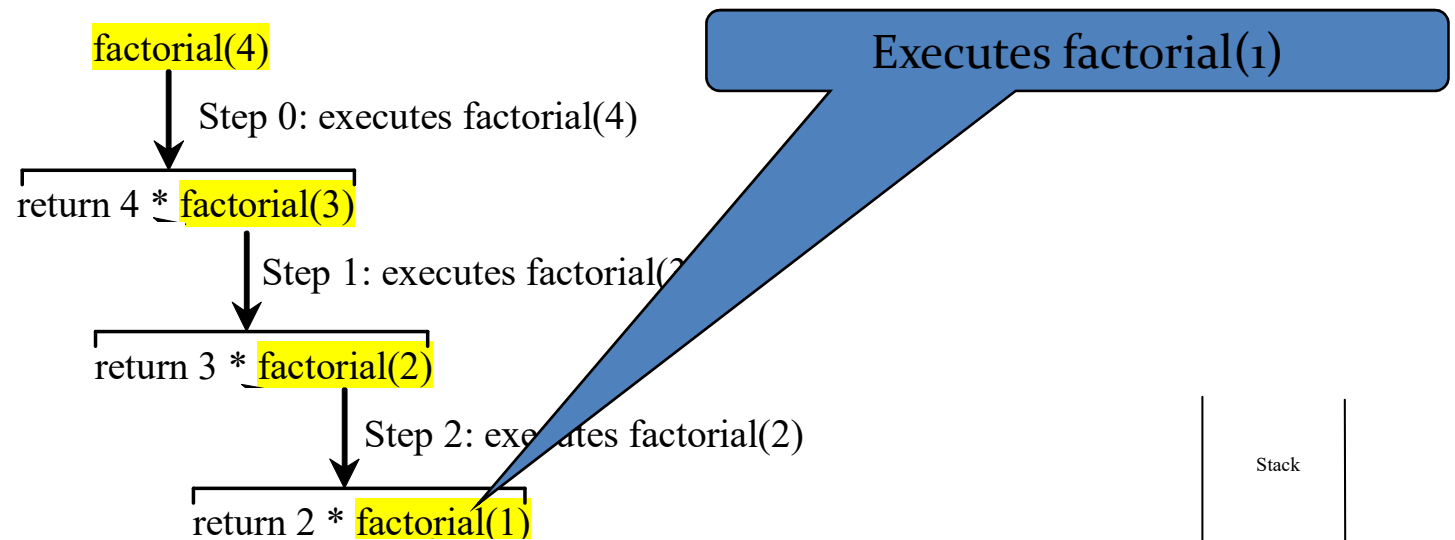


Recursive Factorial



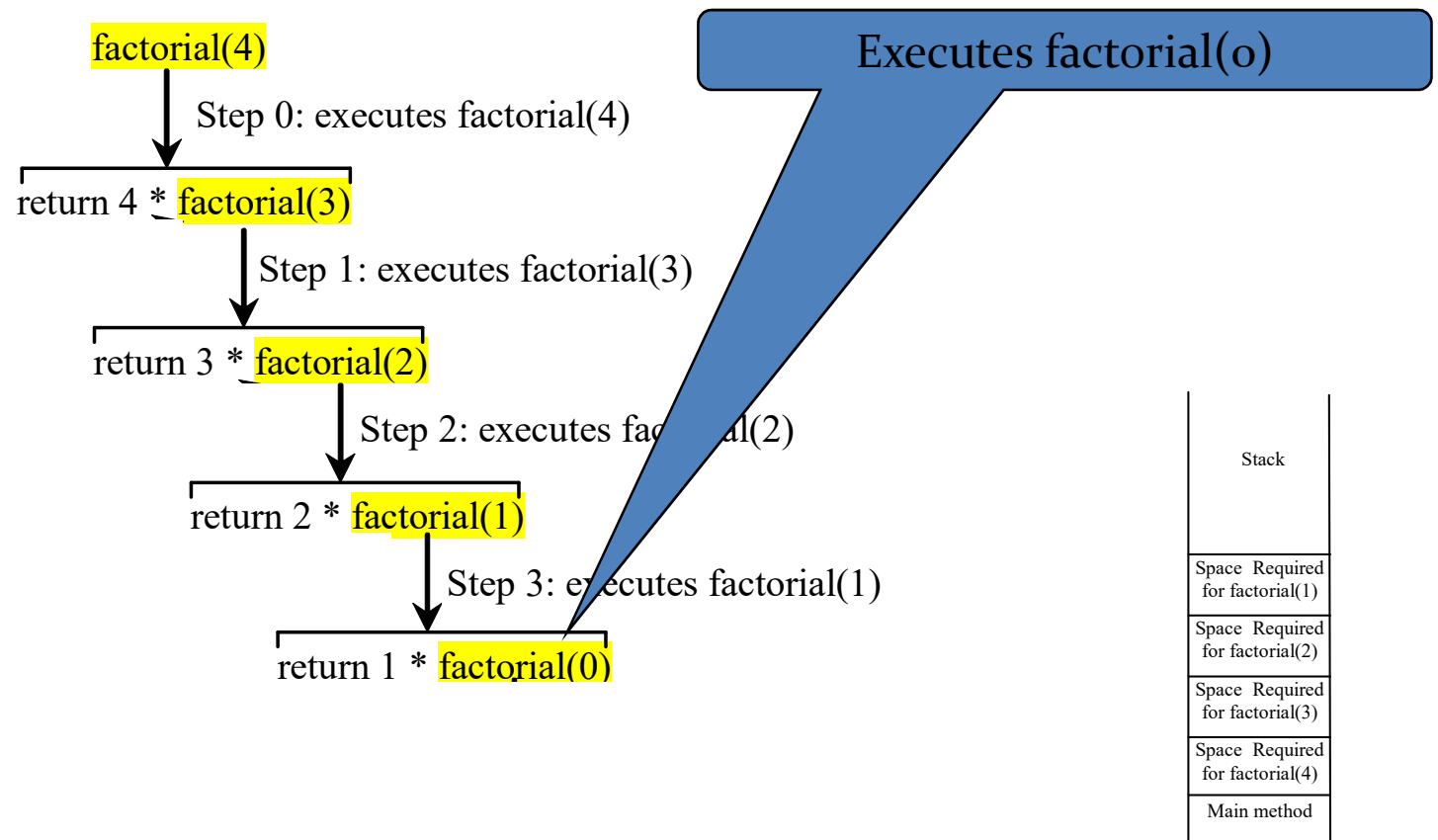
Stack
Space Required for factorial(3)
Space Required for factorial(4)
Main method

Recursive Factorial

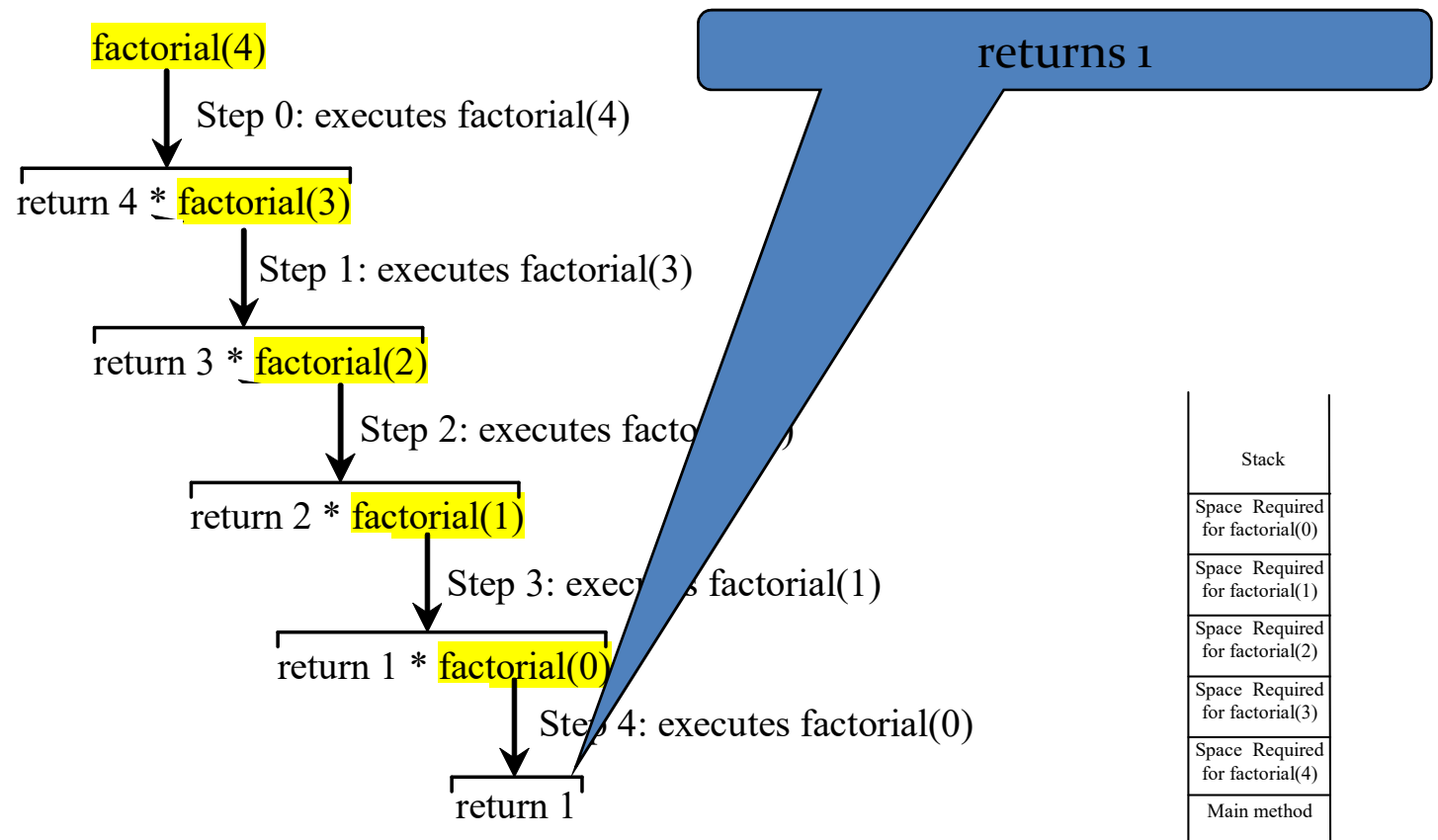


Stack
Space Required for factorial(2)
Space Required for factorial(3)
Space Required for factorial(4)
Main method

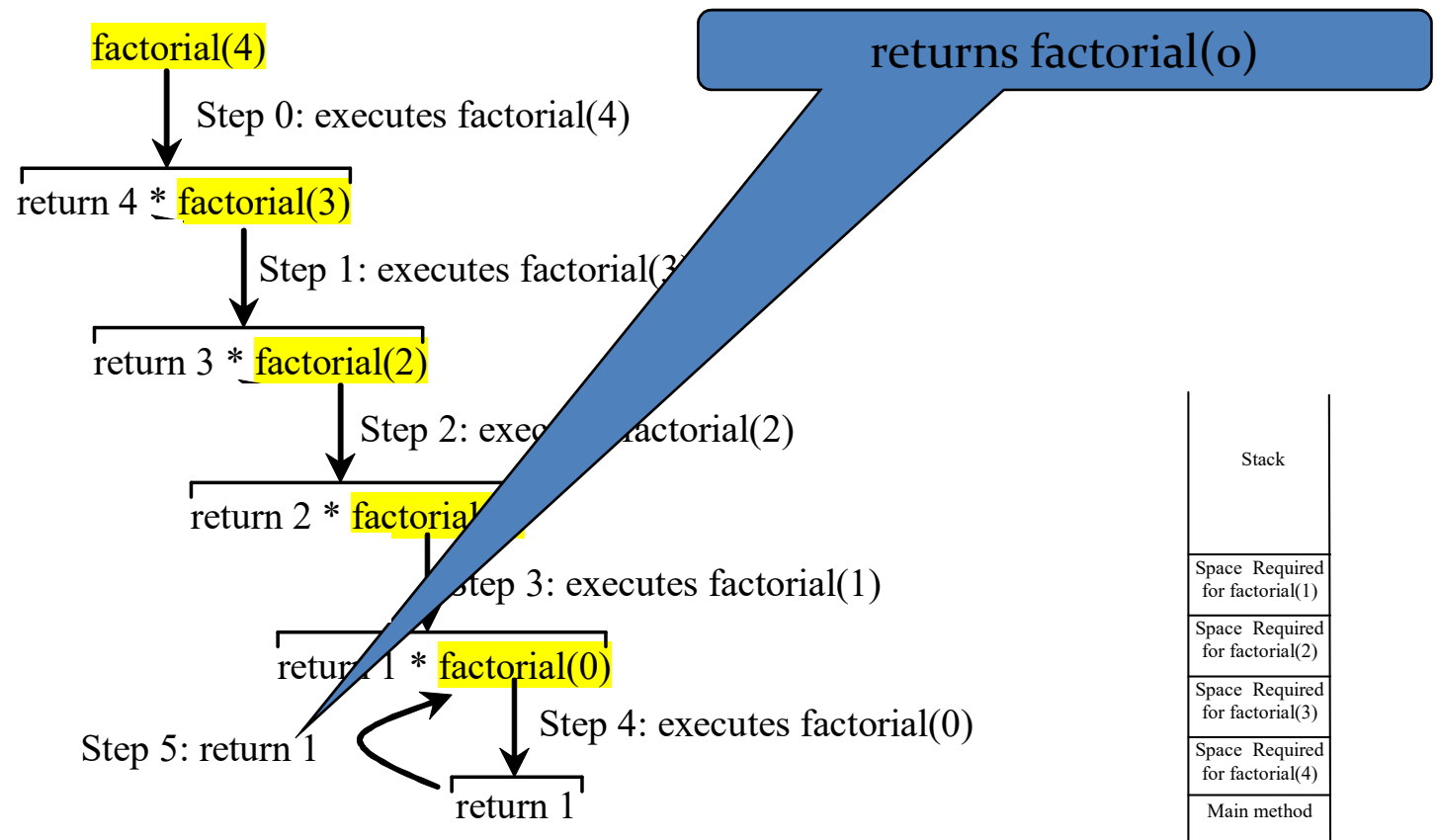
Recursive Factorial



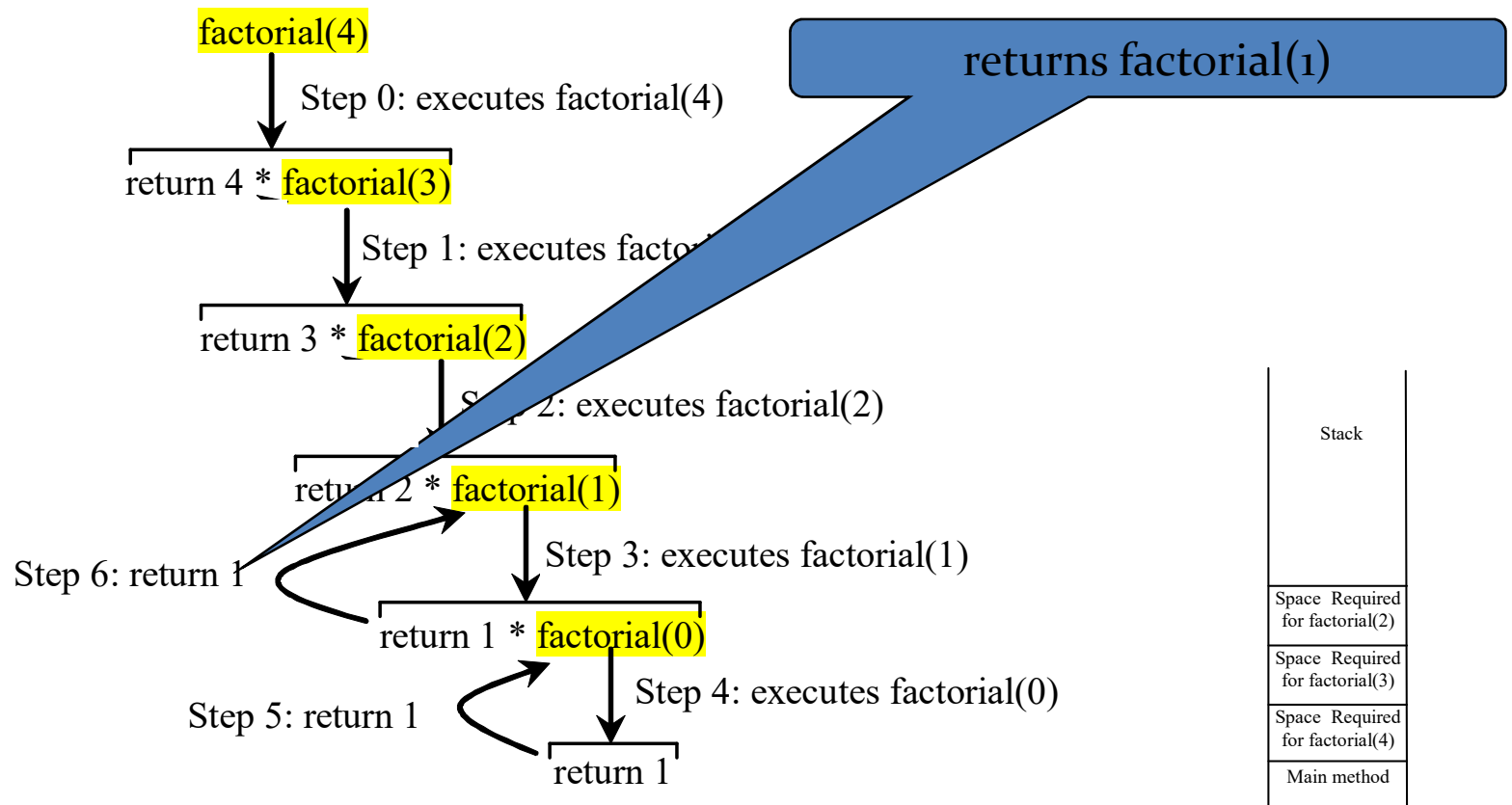
Recursive Factorial



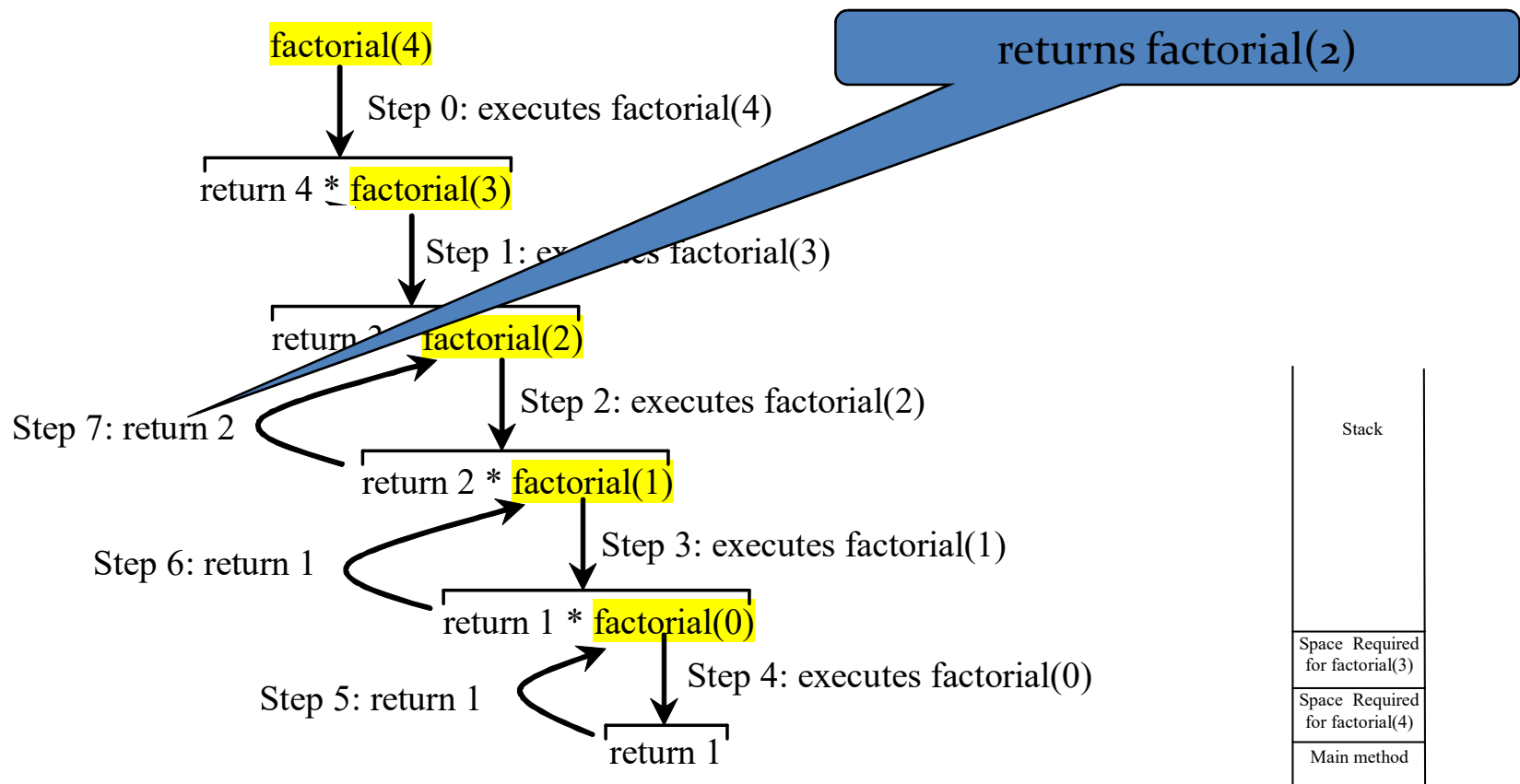
Recursive Factorial



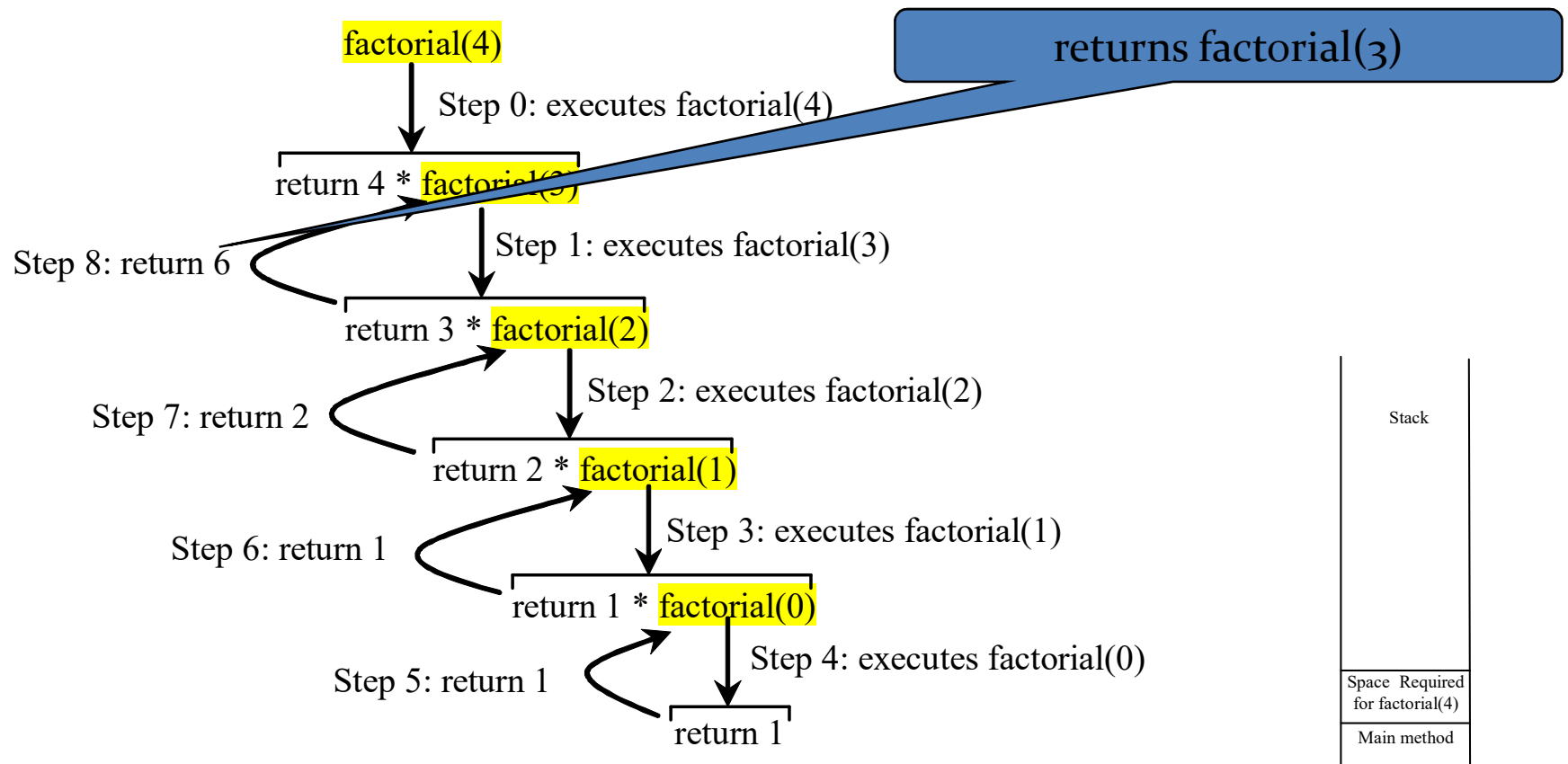
Recursive Factorial



Recursive Factorial



Recursive Factorial



Recursive Factorial

