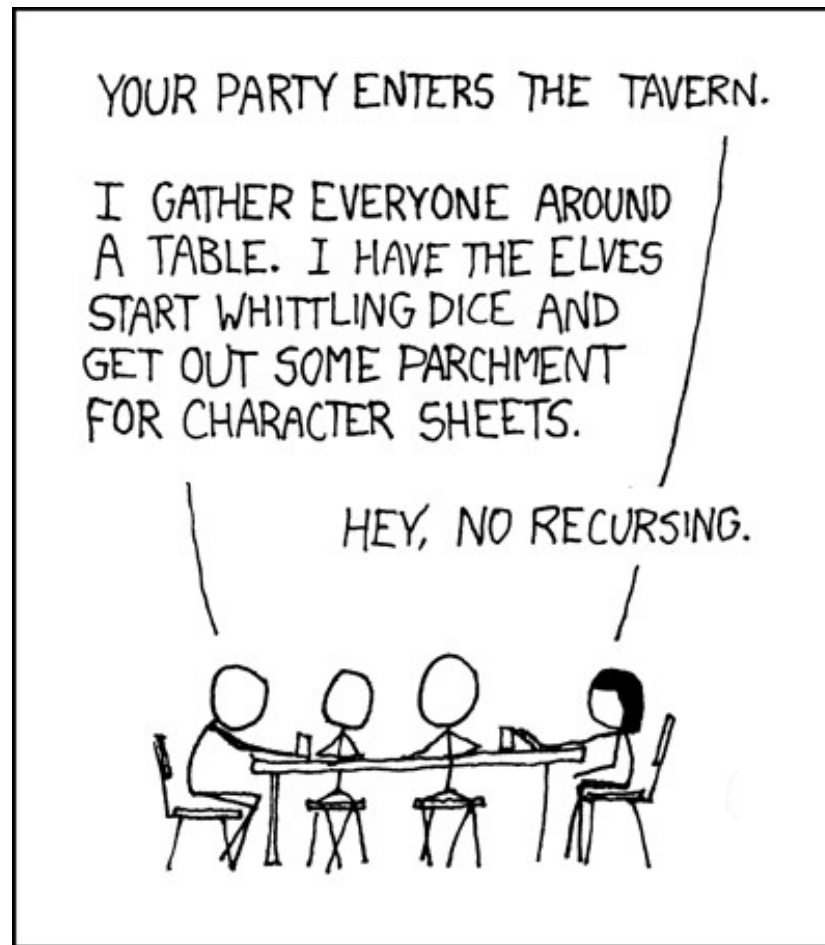


CS 161, Lecture 13: Recursion



What is Recursion?

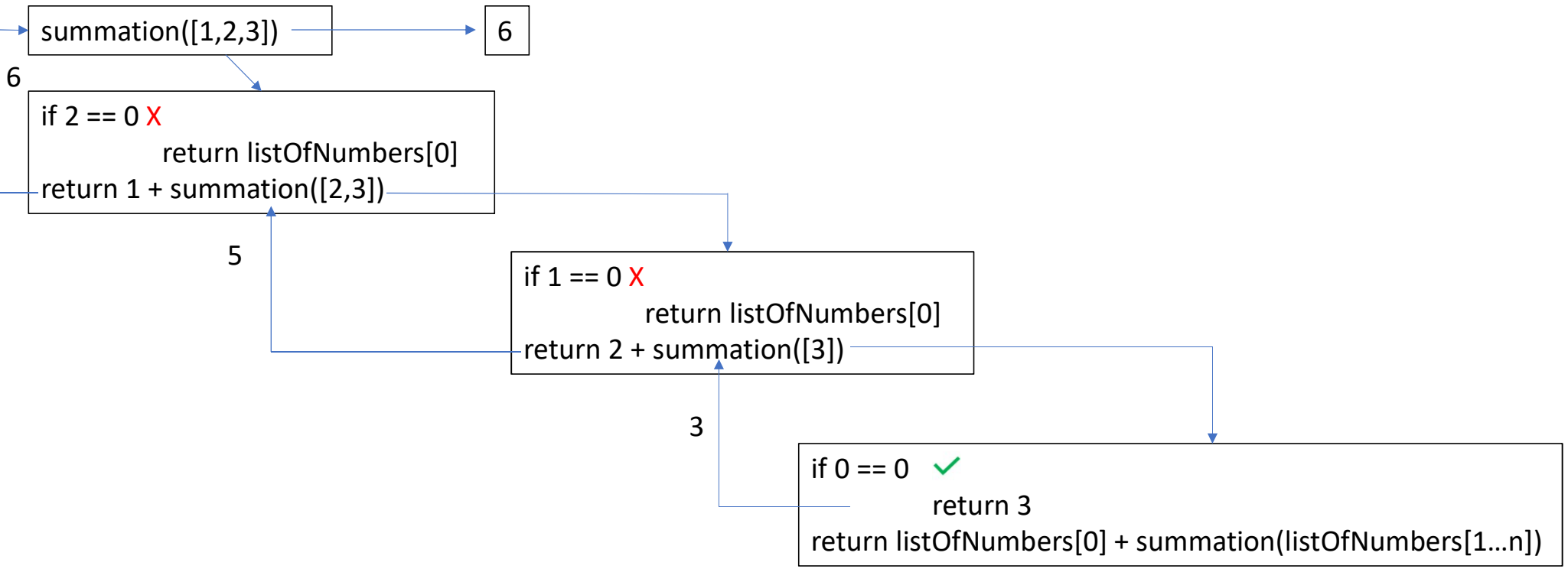
- When a function calls itself one or more times (directly or indirectly)
- Form of repetition
- Typically used to perform same operation on a smaller subset and then build the result based on what is returned from the smaller case
- Typically has at least one base case for stopping
- Based on inductive logic

Iteration vs. Recursion

- Anything that can be done iteratively can be do recursively and vice versa
 - Not always a good idea, some problems naturally lend themselves to one mode of thinking or the other

```
summation(listOfNumbers[0...n])
  if n == 0
    return listOfNumbers[0]
  return listOfNumbers[0] + summation(listOfNumbers[1...n])
```

How it works on a high level



Pros and Cons

- Pros
 - Readable
 - Sometimes easier to conceptualize for problems that have many moving parts
- Cons
 - Efficiency
 - Memory usage
 - Each call to the function makes a new function stack frame (see previous slide)

Example: Factorial

- The product of an integer and all that come before it
- $n! = n * (n-1) * (n-2) * \dots * (n-(n-1)) * 1$ for all $n > 0$
- Base Case: $0! = 1$

Iterative Factorial

$n = 4$

```
int factorial(int n) {  
    int fact;  
    if (n == 0)  
        fact = 1;  
    else  
        for (fact = n; n > 1; n--)  
            fact = fact * (n-1);  
    return fact;  
}
```

Handwritten annotations in red:

- Under `if (n == 0)`, the number `1` is written.
- Under `fact = 1;`, the number `1` is written and crossed out.
- Under `else`, the numbers `3` and `4` are written and crossed out.
- Under `fact = fact * (n-1);`, the numbers `4`, `3`, and `2` are written and crossed out.
- Under `return fact;`, the number `24` is written with an arrow pointing to it.
- Under `return fact;`, the numbers `12` and `24` are written.
- Under `return fact;`, the numbers `4-1`, `3-1`, and `2-1` are written in a list.

Recursive Factorial

$n = 4$

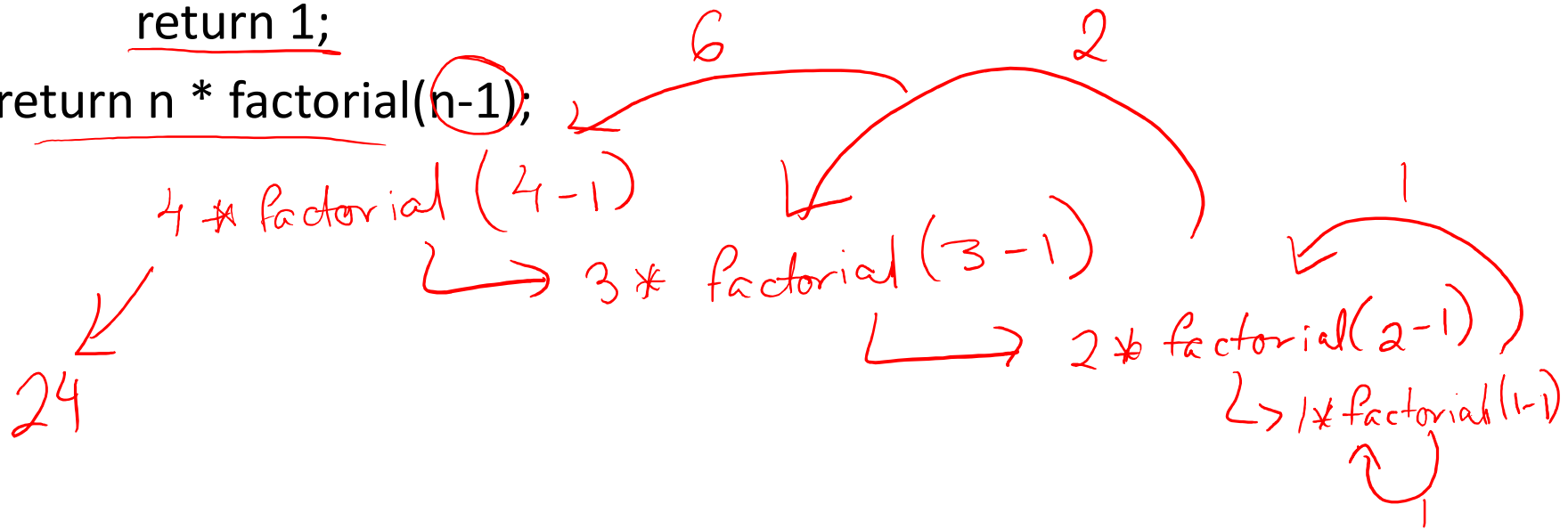
```
int factorial (int n) {
```

```
    if (n == 0)
```

```
        return 1;
```

```
    return n * factorial(n-1);
```

```
}
```



Code Demo

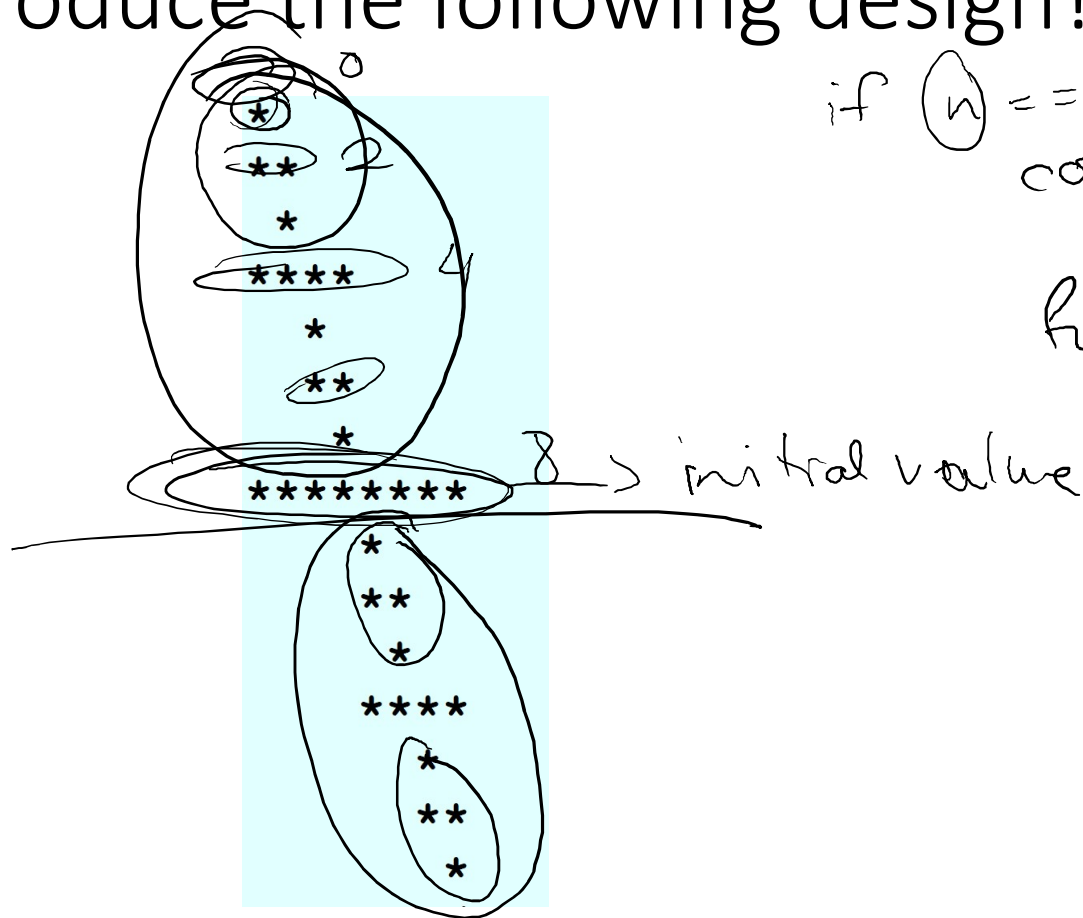
```
access.engr.orst.edu - PuTTY
1 #include <iostream>
2
3 using namespace std;
4
5 int fact_itr(int n) {
6     cout << "Entered the function for n = " << n << endl;
7     int fact;
8     if(n==0)
9         fact = 1;
10    else{
11        for(fact = n; n > 1; n--){
12            fact = fact * (n-1);
13            cout << "Value in for loop: " << fact << endl;
14        }
15    }
16    return fact;
17 }
18
19 int fact_rec(int n) {
20     cout << "Function made for n = " << n << endl;
21     if (n == 0)
22         return 1;
23     int fact = n*fact_rec(n-1);
24     cout << "Returning " << fact << endl;
"fact.cpp" 33L, 592C
24,2-9
Top
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```

```
10     else{
11         for (fact = n; n > 1; n--){
12             fact = fact * (n-1);
13             cout << "Value in for loop: " << fact << endl;
14         }
15     }
16     return fact;
17 }
18
19 int fact_rec(int n) {
20     cout << "Function made for n = " << n << endl;
21     if (n == 0)
22         return 1;
23     int fact = n*fact_rec(n-1);
24     cout << "Returning " << fact << endl;
25     return fact;
26 }
27
28 int main() {
29
30     cout << "Fact iter: " << fact_itr(4) << endl;
31     cout << "Fact rec: " << fact_rec(4) << endl;
32     return 0;
33 }
```

24,2-9

Bot

Exercise: What is the recursive solution to produce the following design?



if $w == 1$
 cout << "*" << endl;

func (n , 0)
 n # stars offset
 $\hookrightarrow 8/2$
 $\hookrightarrow 4/2$
 $\hookrightarrow 2$

```
print (stars, col)
for # of cols
  cout << " " ;
for # of stars
  cout << "*" ;
cout << endl ;
```

```
if (stars == 2)
  print (star, col)
else
```

```
1 #include <iostream>
2
3 using namespace std;
4
5 void print(int stars, int col) {
6     for(int i=0; i<col; i++)
7         cout << " ";
8     for(int i=0; i<stars; i++)
9         cout << "*";
10    cout << endl;
11 }
12
13 void pattern(int stars, int col) {
14     if (stars == 2){
15         print((stars/2), col);
16         cout << "Top if 2" << endl;
17     }
18     else{
19         cout << "Top else" << endl;
20         pattern((stars/2), col);
21         cout << "returned" << endl;
22     }
23     cout << "Mid" << endl;
24     print(stars, col);
```

24,2-9

Top

```
13 void pattern(int stars, int col) {
14     if (stars == 2){
15         print((stars/2), col);
16         cout << "Top if 2" << endl;
17     }
18     else{
19         cout << "Top else" << endl;
20         pattern((stars/2), col);
21         cout << "returned" << endl;
22     }
23     cout << "Mid" << endl;
24     print(stars, col);
25     if (stars == 2){
26         cout << "Bottom if 2" << endl;
27         print((stars/2), col+(stars/2));
28     }
29     else{
30         cout << "Bottom else" << endl;
31         pattern((stars/2), col+(stars/2));
32         cout << "returned" << endl;
33     }
34 }
35
36
```

```
22     }
23     cout << "Mid" << endl;
24     print(stars, col);
25     if (stars == 2){
26         cout << "Bottom if 2" << endl;
27         print((stars/2), col+(stars/2));
28     }
29     else{
30         cout << "Bottom else" << endl;
31         pattern((stars/2), col+(stars/2));
32         cout << "returned" << endl;
33     }
34 }
35
36
37 int main () {
38
39     pattern(8, 0);
40     return 0;
41 }
```

```
~
~
~
~
```

24,2-9

Bot