

# **CS 161**

## **Intro to CS I**

Finish Recursion/Begin Memory Model

# Odds and Ends

- Assignment 5 posted
- Assignment 4 demo this week



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# Iterative Factorial



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factorial(0) = 1;

factorial(n) =  $n * n-1 * n-2 * \dots * n-(n-1) * 1$ ;

```
long factorial(int n) {  
    long fact;  
    if(n==0)  
        fact=1;  
    else  
        for(fact=n; n > 1; n--)  
            fact=fact*(n-1);  
    return fact;  
}
```

# Recursive Factorial

```
factorial(0) = 1;  
factorial(n) = n*factorial(n-1);
```

```
long factorial(int n) {  
    if (n == 0)    // Base case  
        return 1;  
    else  
        return n * factorial(n - 1);    // Recursive call  
}
```

# Computing Factorial Iteratively



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factorial(4)

```
factorial(0) = 1;
```

```
factorial(n) = n*(n-1)*...*2*1;
```

# Computing Factorial Iteratively



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$$\text{factorial}(4) = 4 * 3$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

# Computing Factorial Iteratively



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$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

# Computing Factorial Iteratively



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$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2 \\ &= 24 * 1\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```



# Computing Factorial Iteratively



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$$\begin{aligned}\text{factorial}(4) &= 4 * 3 \\ &= 12 * 2 \\ &= 24 * 1 \\ &= 24\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

# Computing Factorial Recursively



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factorial(4)

```
factorial(0) = 1;
```

```
factorial(n) = n*factorial(n-1);
```

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\text{factorial}(4) = 4 * \text{factorial}(3)$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \end{aligned}$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * ( 3 * \text{factorial}(2) ) \\ &= 4 * ( 3 * ( 2 * \text{factorial}(1) ) )\end{aligned}$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * ( 3 * \text{factorial}(2) ) \\ &= 4 * ( 3 * ( 2 * \text{factorial}(1) ) ) \\ &= 4 * ( 3 * ( 2 * ( 1 * \text{factorial}(0) ) ) ) \end{aligned}$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1)))\end{aligned}$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1))\end{aligned}$$



# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \end{aligned}$$

# Computing Factorial Recursively



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```
factorial(0) = 1;  
factorial(n) = n * factorial(n-1);
```

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \\ &= 4 * 6 \end{aligned}$$

# Computing Factorial Recursively



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`factorial(0) = 1;`

`factorial(n) = n*factorial(n-1);`

$$\begin{aligned} \text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \\ &= 4 * 6 \\ &= 24 \end{aligned}$$

# Differences

- Pros
  - Readability
- Cons
  - Efficiency
  - Memory



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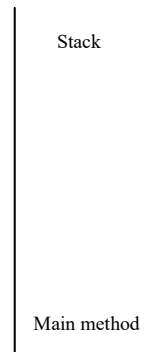
# Recursive Factorial



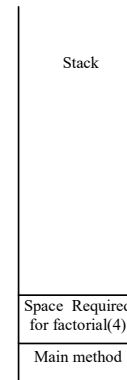
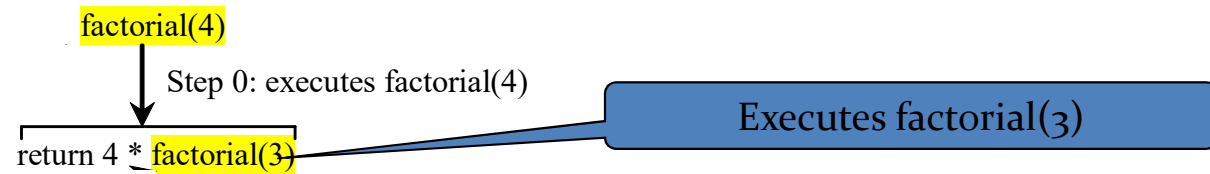
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factorial(4)

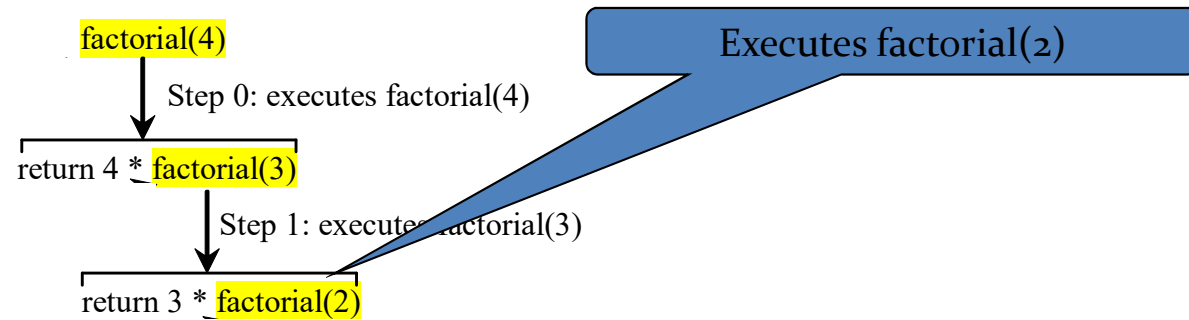
Executes factorial(4)



# Recursive Factorial

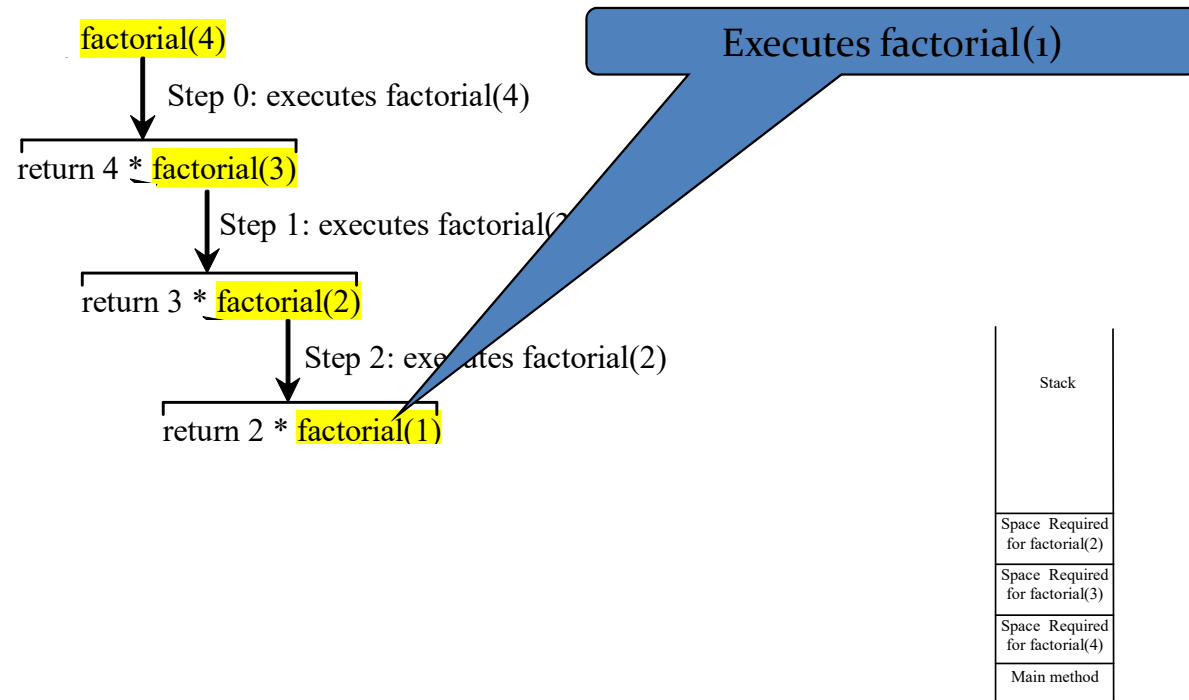


# Recursive Factorial



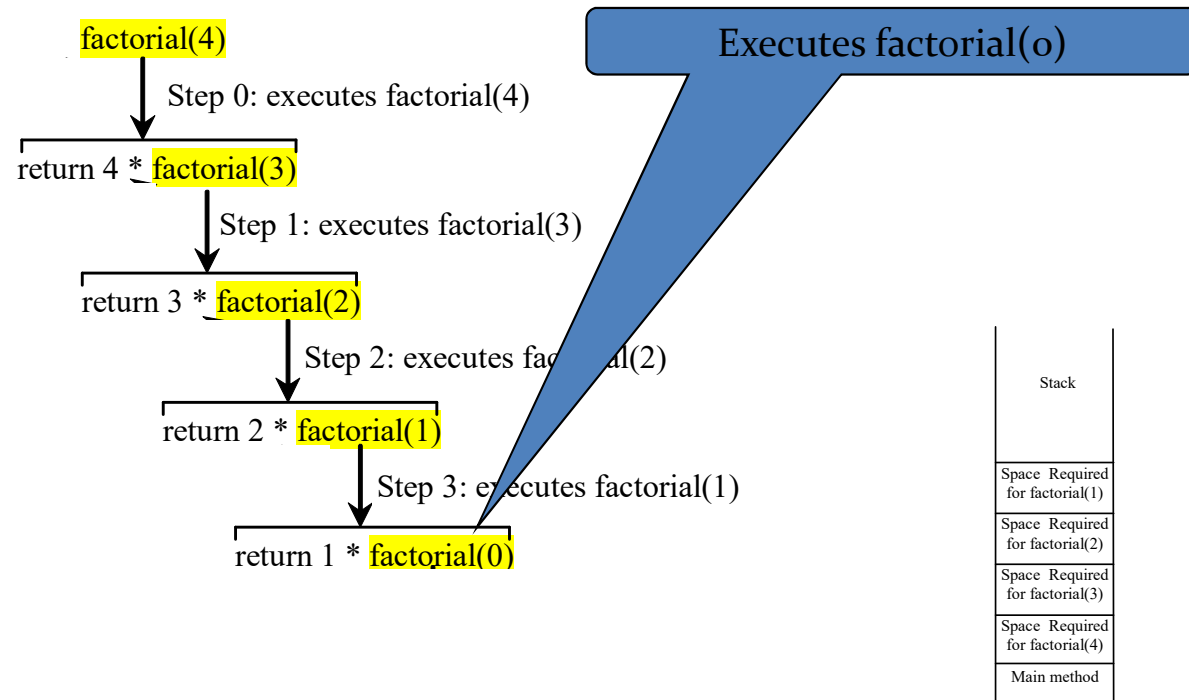
Stack
Space Required for factorial(3)
Space Required for factorial(4)
Main method

# Recursive Factorial

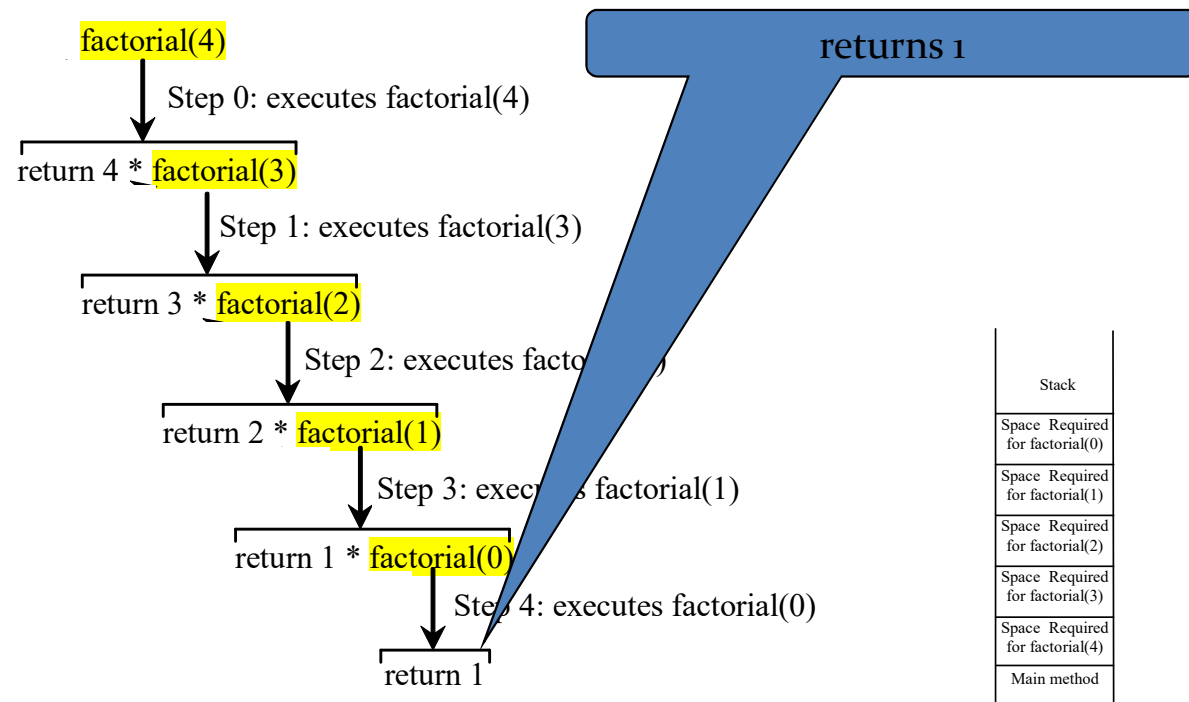




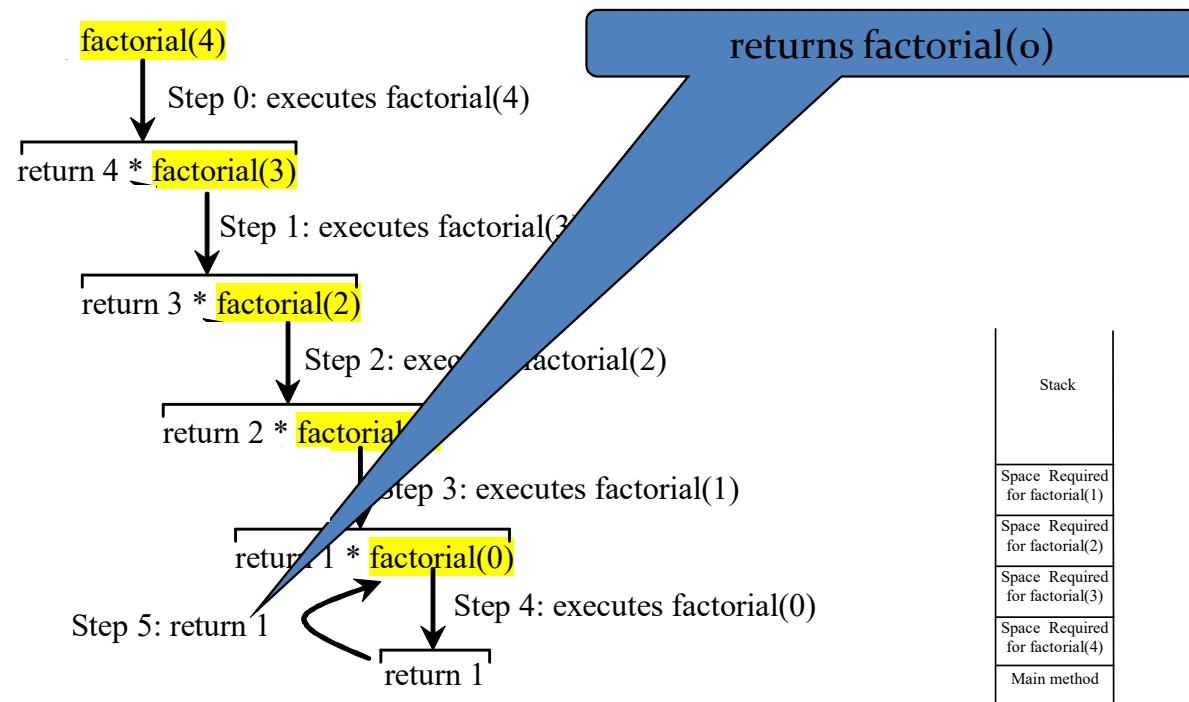
# Recursive Factorial



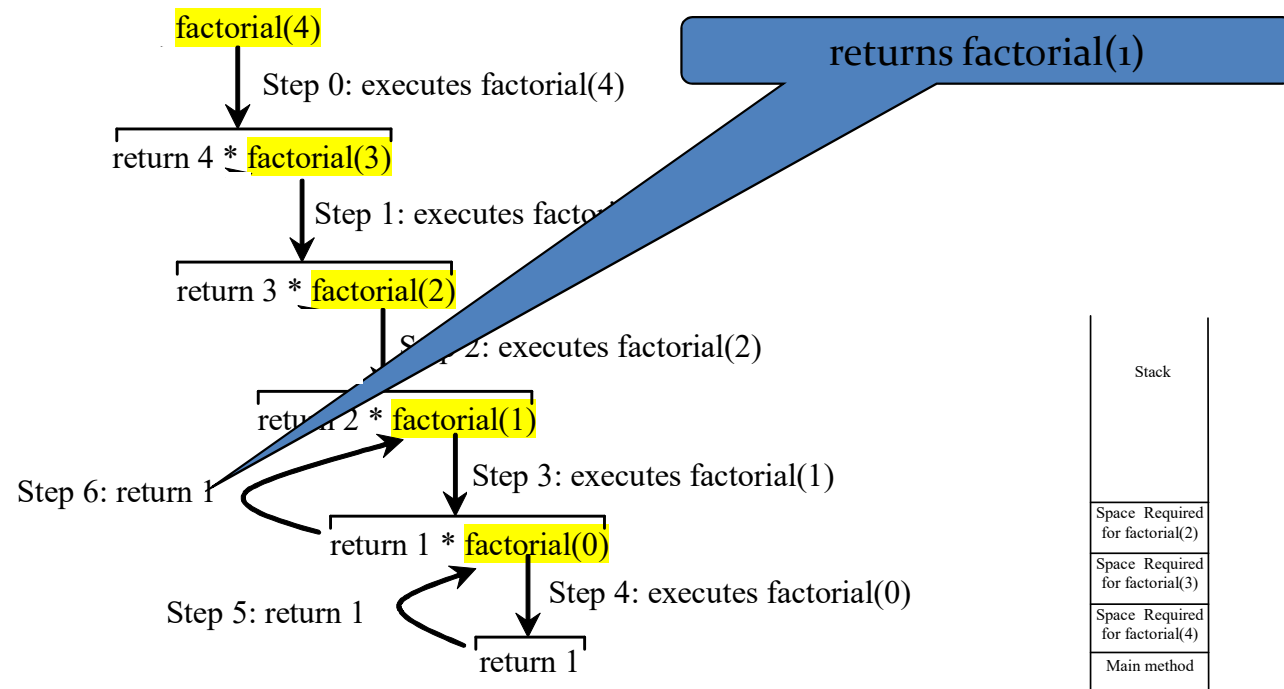
# Recursive Factorial



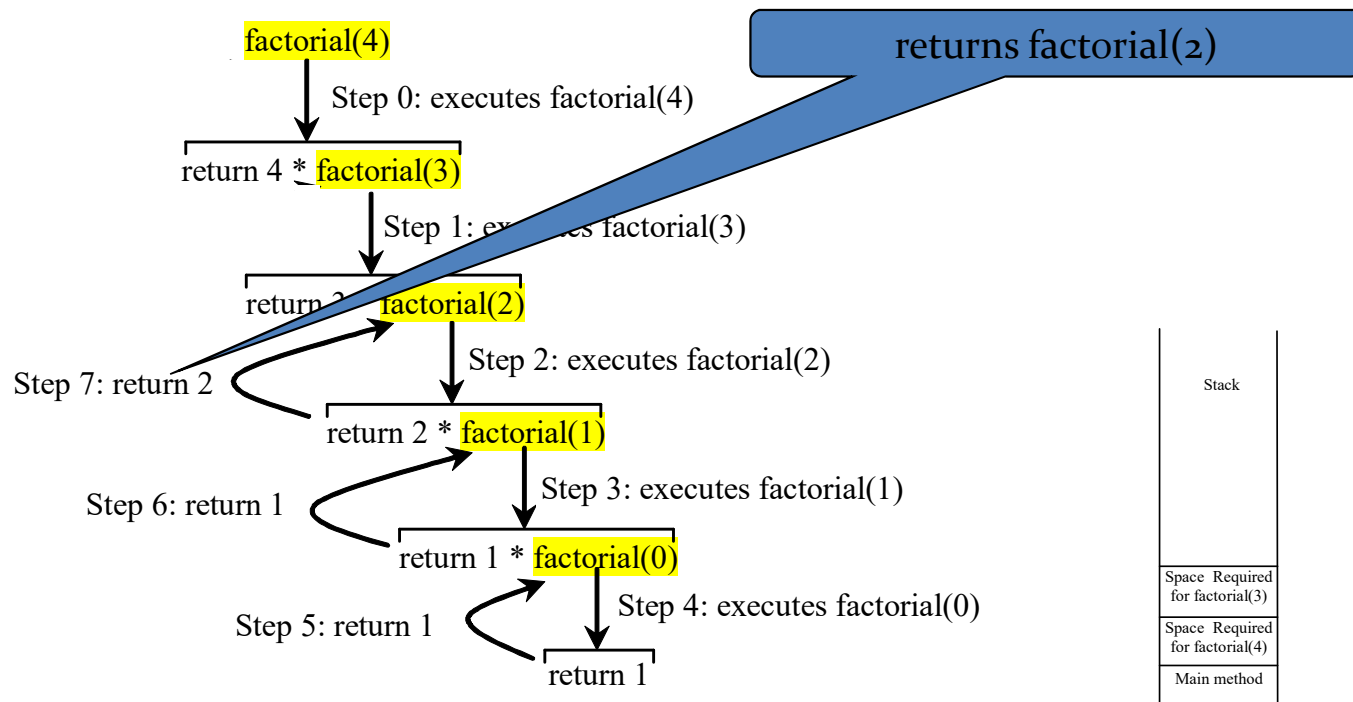
# Recursive Factorial



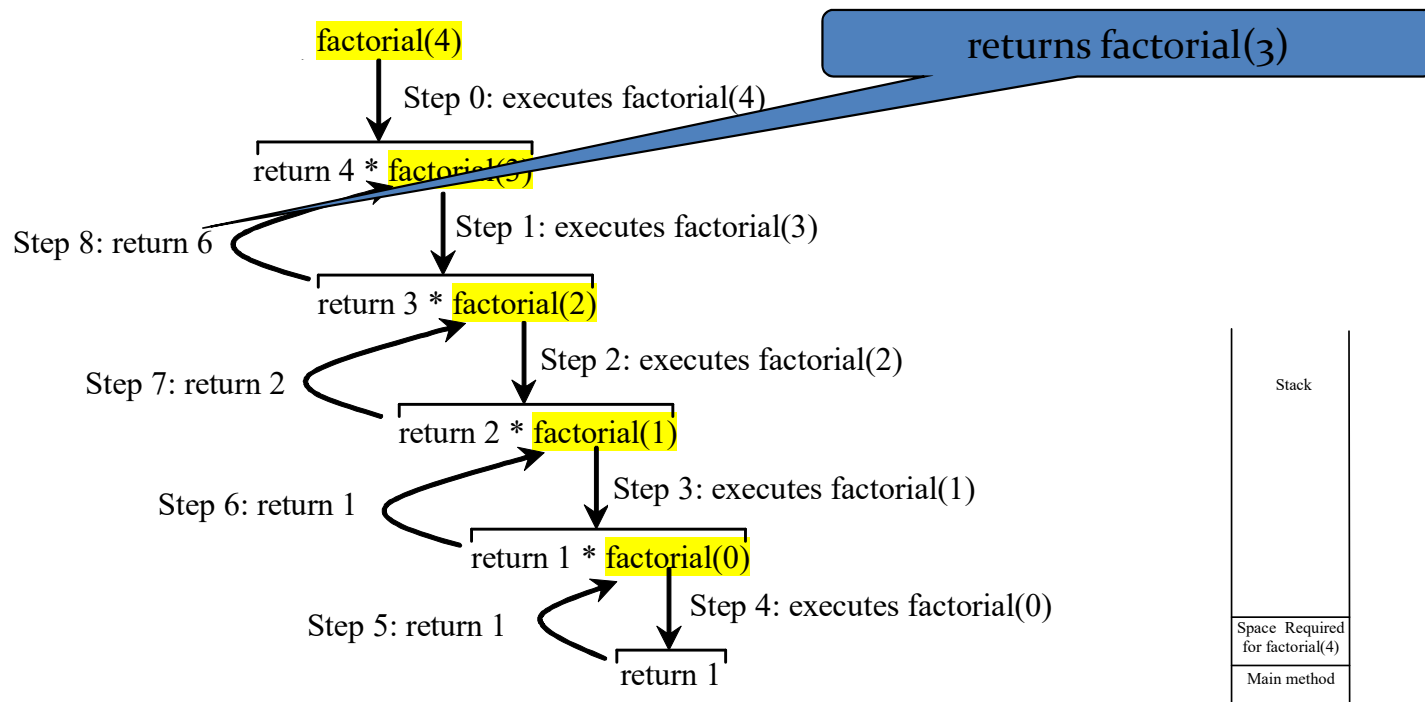
# Recursive Factorial



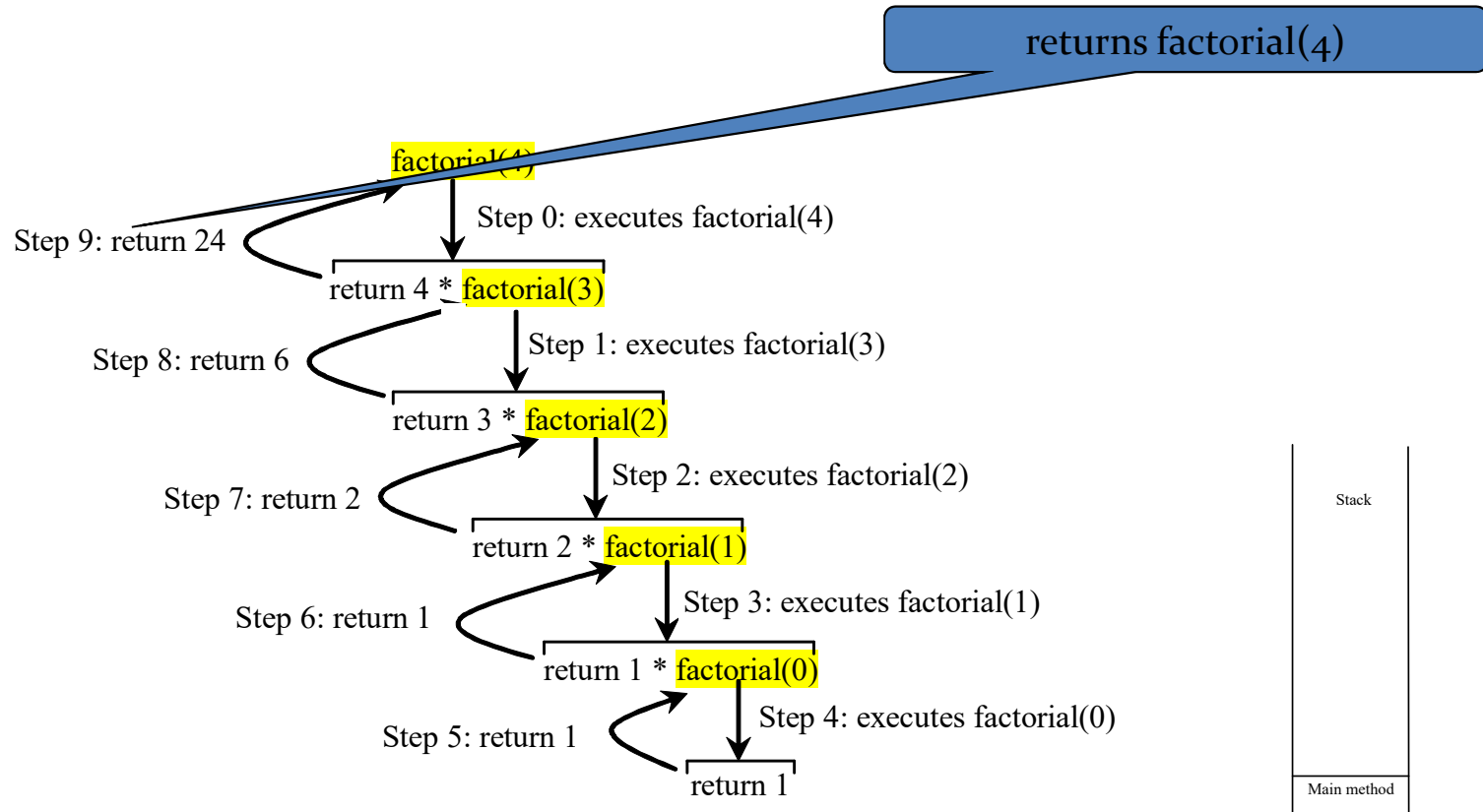
# Recursive Factorial



# Recursive Factorial



# Recursive Factorial



# In-class Exercise #4



- Get into groups of 4 – 5.
- Write your own recursive *int pwr()* function that takes two integers as arguments and returns the integer result.
  - What does the function prototype look like?
  - Now, write the function definition...



# Stack vs. Heap

- Static vs. Dynamic



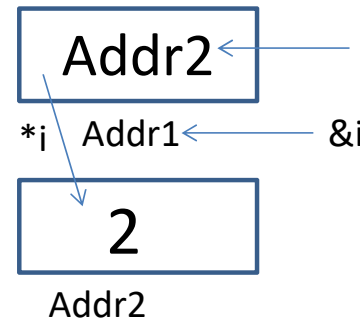
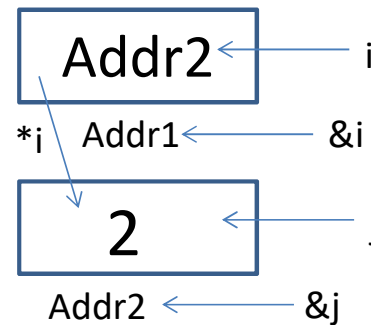
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# Static vs. Dynamic

- Static Semantics
  - Assign address of variable

```
int *i, j=2;  
i=&j;
```
- Dynamic Semantics
  - Create memory
  - Assign memory to pointer

```
int *i=NULL;  
i=new int;  
*i=2;
```





# What About Memory Leaks?

- What happens here...

...

```
int main () {  
    int *i=NULL;    //created in main function  
    while(1) {  
        i = new int;  
    }  
}
```

# Fixing Memory Leaks...



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- What happens here...

...

```
int main () {  
    int *i=NULL;    //created in main function  
    while(1) {  
        i = new int;  
        delete i; //free memory that i points to, preventing mem leaks  
    }  
}
```

# Dynamic Memory Demo...



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