CS 331: Artificial Intelligence Propositional Logic I

Knowledge-based Agents

- Can represent knowledge
- And reason with this knowledge
- How is this different from the knowledge used by problem-specific agents?
 - More general
 - More flexible

Outline

- 1. Knowledge-based Agents
- 2. The Wumpus World
- 3. Logic

Knowledge-based Agents

- Knowledge of problem solving agents is specific and inflexible
- Knowledge-based agents can benefit from knowledge expressed in very general forms, combining information in different ways to suit different purposes
- Knowledge-based agents can combine general knowledge with current percepts to infer hidden aspects of the current state

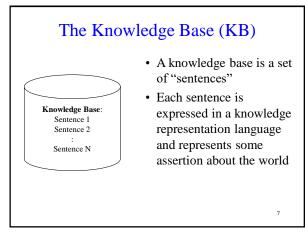
Knowledge-based Agents

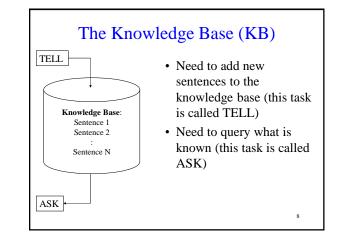
Flexibility of knowledge-based agents:

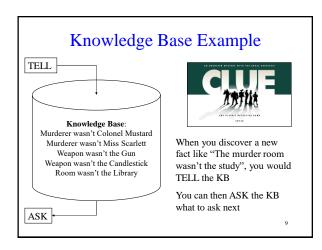
- Accept new tasks in the form of explicitly described goals
- Achieve competence quickly by being told or learning new knowledge about the environment
- Adapt to changes in the environment by updating the relevant knowledge

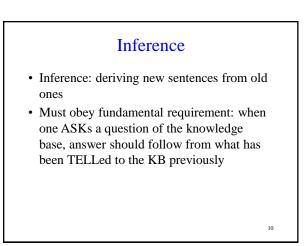
Knowledge is definite

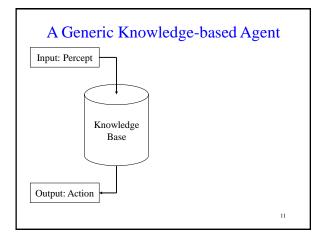
- Knowledge of logical agents is always definite
- That is, each proposition is entirely true or entirely false
- Agent may be agnostic about some propositions
- · Logic doesn't handle uncertainty well

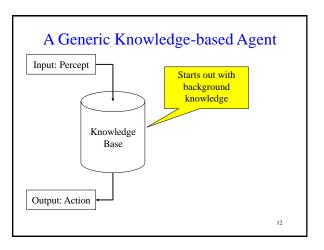


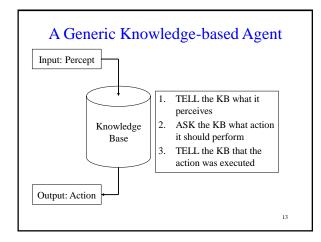




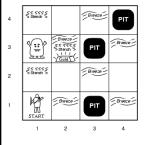








The Wumpus World



- Wumpus eats anyone that enters its room
- Wumpus can be shot by an agent, but agent has one arrow
- Pits trap the agent (but not the wumpus)
- Agent's goal is to pick up the gold

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The Wumpus World

Performance measure:

- +1000 for picking up gold, -1000 for death (meeting a live wumpus or falling into a pit)
- -1 for each action taken, -10 for using arrow
- Environment:
 - -4x4 grid of rooms
 - Agent starts in (1,1) and faces right
 - Geography determined at the start:
 - Gold and wumpus locations chosen randomlyEach square other than start can be a pit with
 - probability 0.2

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The Wumpus World

- Actuators:
 - Movement:
 - Agent can move forward
 - Turn 90 degrees left or right
 - Grab: pick up an object in same square
 - Shoot: fire arrow in straight line in the direction agent is facing

The Wumpus World

Sensors:

- Returns a 5-tuple of five symbols eg. [stench, breeze, glitter, bump, scream] (note that in this 5-tuple, all five things are present. We indicate absence with the value None)
- In squares adjacent to the wumpus, agent perceives a stench
- In squares adjacent to a pit, agent perceives a breeze
- In squares containing gold, agent perceives a glitter
- When agent walks into a wall, it perceives a bump
- When wumpus is killed, it emits a woeful scream that is perceived anywhere

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The Wumpus World

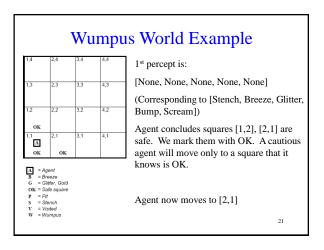
- Biggest challenge: Agent is ignorant of the configuration of the 4x4 world
- Needs logical reasoning of percepts in order to overcome this ignorance
- Note: retrieving gold may not be possible due to randomly generated location of pits
- Initial knowledge base contains:
 - Agent knows it is in [1,1]
 - Agent knows it is a safe square

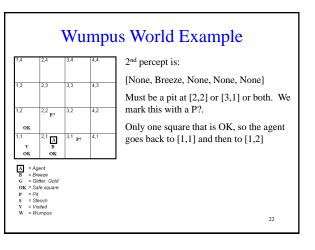
The Wumpus World Environment Properties

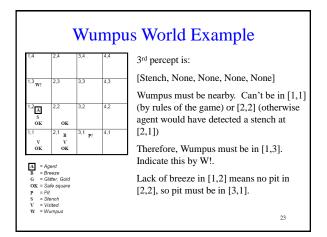
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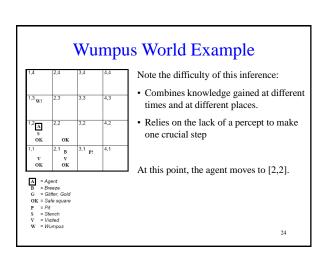
- Fully or Partially observable?
- Deterministic or stochastic?
- Episodic or sequential?
- Static or dynamic?
- Discrete or continuous?
- Single agent or multiagent?

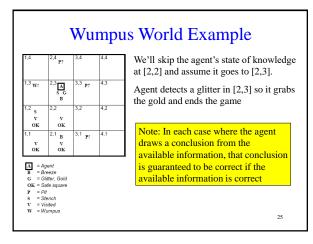
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Logic

Logic must define:

- 1. Syntax of the representation language Symbols, rules, legal configurations
- 2. Semantics of the representation language
 - Loosely speaking, this is the "meaning" of the sentence

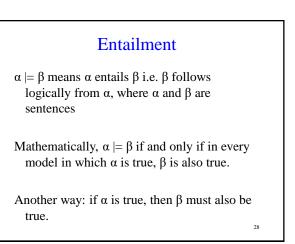
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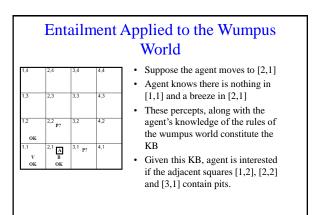
- Defines the truth of each sentence with respect to each possible world
- Everything is either true or false, no in between

Models

- We will use the word model instead of "possible world"
- "m is a model of α " means that sentence α is true in model m
- Models are mathematical abstractions which fix the truth or falsehood of every relevant sentence
- Think of it as the possible assignments of values to the variables
 - assignments of numbers to x and y such that they add up to 4

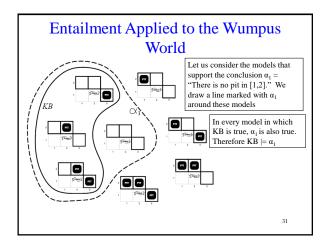
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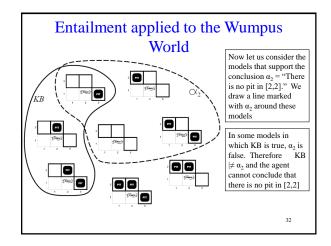




Entailment Applied to the Wumpus World $2^3 = 8$ possible models because [1,2], [2,2] and [3,1] can take each take values true or false that there is a pit there The 3 models inside the line marked KB are those in which the KB is true 30

- E.g. the possible models for x + y = 4 are all possible



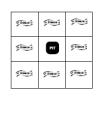


Logical inference

- Entailment can be applied to derive conclusions (we call this carrying out logical inference)
- Model checking: enumerates all possible models to check that α is true in all models in which KB is true
- If an inference algorithm *i* can derive α from the KB, we write KB |- i α
- The above is pronounced "α is derived from KB by *i*" or "*i* derives α from KB"

Modified Wumpus World

• Breeze occurs in squares directly or diagonally adjacent to a pit



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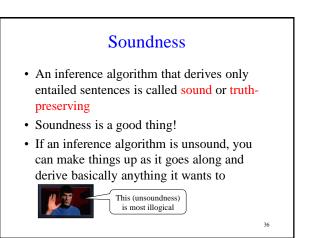
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OK

• Want to reason about squares [2,2], [2,3], [1,3]

OK

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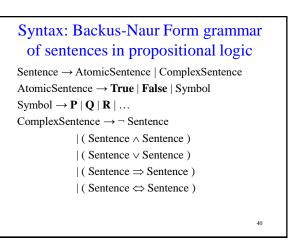
Completeness

- An inference algorithm is complete if it can derive any sentence that is entailed
- For some KBs, the number of sentences can be infinite
- Can't exhaustively check all of them, need to rely on proving completeness

In Summary

- Soundness: *i* is sound if whenever KB $|-_i \alpha$, it is also true that KB $|= \alpha$
- Completeness: *i* is complete if whenever *KB* $\mid = \alpha$, it is also true that *KB* $\mid -i \alpha$

Propositional Logic: Syntax and Semantics



Atomic Sentences

- · The indivisible syntactic elements
- Consist of a single propositional symbol e.g. P, Q, R that stands for a proposition that can be true or false e.g. P=true, Q=false
- We also call an atomic sentence a literal
- 2 special propositional symbols:
 - True (the always true proposition)
 - False (the always false proposition)

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- Made up of sentences (either complex or atomic)
- 5 common logical connectives:
 - \neg (not): negates a literal
 - \wedge (and): conjunction e.g. $P \wedge Q$ where P and Q are called the conjuncts
 - $\lor (or)$: disjunction e.g. $P \lor Q$ where P and Q are called the disjuncts
 - → (implies): e.g. P ⇒ Q where P is the premise/antecedent and Q is the conclusion/consequent
 - \Leftrightarrow (if and only if): e.g. $P \Leftrightarrow Q$ is a biconditional

Precedence of Connectives

- In order of precedence, from highest to lowest: ¬, ∧, ∨, ⇒, ⇔
- E.g. $\neg P \lor Q \land R \Rightarrow S$ is equivalent to ($(\neg P) \lor (Q \land R)$) $\Rightarrow S$
- You can rely on the precedence of the connectives or use parentheses to make the order explicit
- Parentheses are necessary if the meaning is ambiguous

Semantics (Are sentences true?)

- Defines the rules for determining if a sentence is true with respect to a particular model
- For example, suppose we have the following model: P=true, Q=false, R=true
- Is $(P \land Q \land R)$ true?



Semantics

For atomic sentences:

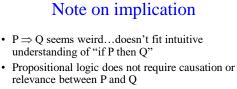
- True is true, False is false
- A symbol has its value specified in the model

For complex sentences (for any sentence S and model m):

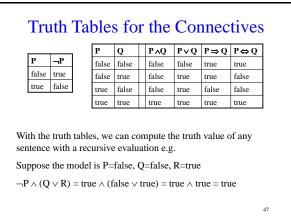
- $\neg S$ is true in m iff S is false in m
- $S_1 \wedge S_2$ is true in m iff S_1 is true in m and S_2 is true in m
- $S_1 \vee S_2$ is true in m iff S_1 is true in m or S_2 is true in m
- $S_1 \Rightarrow S_2$ is true in m iff S_1 is false in m or S_2 is true in m i.e., can translate it as $\neg S_1 \lor S_2$
- $S_1 \Leftrightarrow S_2$ is true iff $S_1 \Rightarrow S_2$ is true in m and $S_2 \Rightarrow S_1$ is true in m

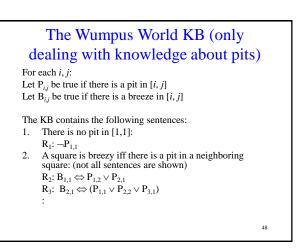
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- Implication is true whenever the antecedent is false (remember $P \Rightarrow Q$ can be translated as $\neg P \lor Q$)
 - Implication says "if P is true, then I am claiming that Q is true. Otherwise I am making no claim"
 - The only way for this to be false is if P is true but Q is false





The Wumpus World KB

3. We add the percepts for the first two squares ([1,1] and [2,1]) visited in the Wumpus World example:

 $R_4: \neg B_{1,1}$ $R_5: B_{2,1}$

 \mathbf{K}_{5} . $\mathbf{D}_{2,1}$

The KB is now a conjunction of sentences $R_1 \wedge R_2 \wedge R_3 \wedge R_4 \wedge R_5$ because all of these sentences are asserted to be true.

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Inference

- How do we decide if KB $\models \alpha$?
- Enumerate the models, check that α is true in every model in which KB is true

B _{1,1}	B _{2,1}	P _{1,1}	P _{1,2}	P _{2,1}	P _{2,2}	P _{3,1}	R ₁	R_2	R ₃	R_4	R ₅	KB
false	true	true	true	true	false	false						
false	false	false	false	false	false	true	true	true	false	true	false	false
:	:	:	:	:	:	:	:	:	:	:	:	:
false	true	false	false	false	false	false	true	true	false	true	true	false
false	true	false	false	false	false	true	true	true	true	true	true	true
false	true	false	false	false	true	false	true	true	true	true	true	true
false	true	false	false	false	true	true	true	true	true	true	true	true
false	true	false	false	true	false	false	true	false	false	true	true	false
:	:	:	:	:	:	:	:	:	:	:	:	:
true	false	true	true	false	true	false						

Inference

• Suppose we want to know if $KB \models \neg P_{1,2}$?

• In the 3 models in which KB is true, $\neg P_{1,2}$ is also true

B _{1,1}	B _{2,1}	P _{1,1}	P _{1,2}	P _{2,1}	P _{2,2}	P _{3,1}	R ₁	R ₂	R ₃	R_4	R ₅	KB
false	true	true	true	true	false	false						
false	false	false	false	false	false	true	true	true	false	true	false	false
:	:	:	:	:	:	:	:	:	:	:	:	:
false	true	false	false	false	false	false	true	true	false	true	true	false
false	true	false	false	false	false	true	true	true	true	true	true	true
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:	:	:	:	:	:	:	:	:	:	:	:	:
true	false	true	true	false	true	false						

Things you should know

- Properties of a knowledge-based agent
- What a knowledge-base is
- What entailment and inference mean
- Desirable properties of inference algorithms such as soundness and completeness