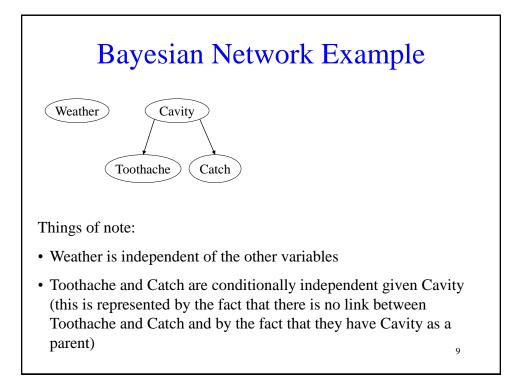
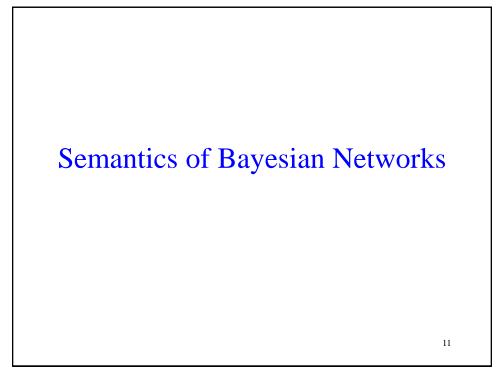


How many entries are independently specifiable?



		Card	P(Card Coin)	Card	Candy	P(Candy Card)
.5	tails	black	0.6	black	1	0.5
.5	tails	red	0.4	black	2	0.2
	heads	black	0.3	black	3	0.3
	heads	red	0.7	red	1	0.1
•			I	red	2	0.3
				red	3	0.6
	5	heads	heads black	heads black 0.3	heads black 0.3 black heads red 0.7 red	heads black 0.3 heads red 0.7 red 1 red 2



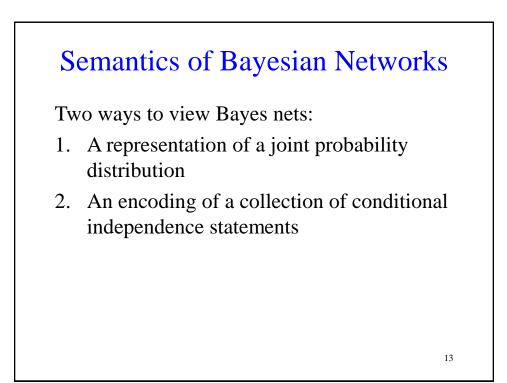
Bayes Nets Formalized

A Bayes net (also called a belief network) is an augmented directed acyclic graph, represented by the pair V , E where:

- V is a set of vertices.
- E is a set of directed edges joining vertices. No loops of any length are allowed.

Each vertex in V contains the following information:

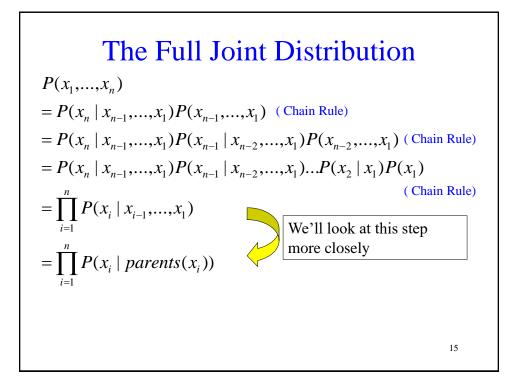
- The name of a random variable
- A probability distribution table indicating how the probability of this variable's values depends on all possible combinations of parental values.



A Representation of the Full Joint Distribution

- We will use the following abbrevations:
 - $P(x_1, ..., x_n)$ for $P(X_1 = x_1 \land ... \land X_n = x_n)$
 - $parents(X_i)$ for the values of the parents of X_i
- From the Bayes net, we can calculate:

$$P(x_1,...,x_n) = \prod_{i=1}^n P(x_i \mid parents(X_i))$$



The Full Joint Distribution $\prod_{i=1}^{n} P(x_i \mid x_{i-1},...,x_1) = \prod_{i=1}^{n} P(x_i \mid parents(x_i))$

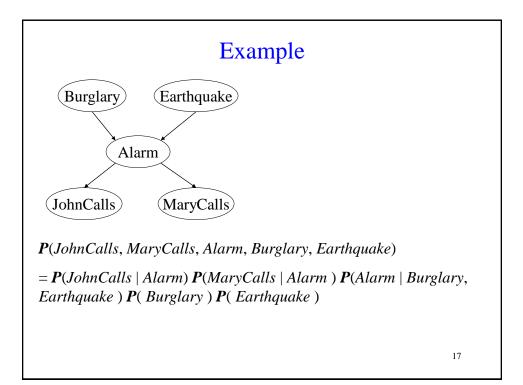
To be able to do this, we need two things:

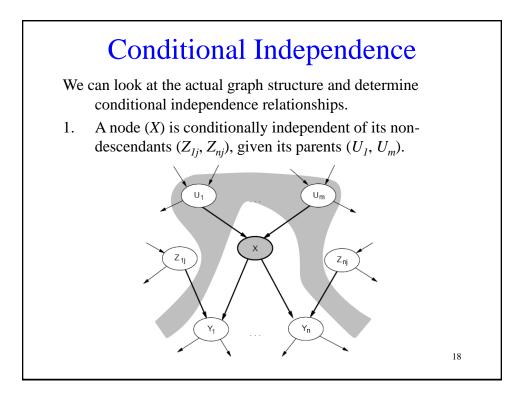
1. $Parents(X_i) \subseteq \{X_{i-1}, ..., X_1\}$

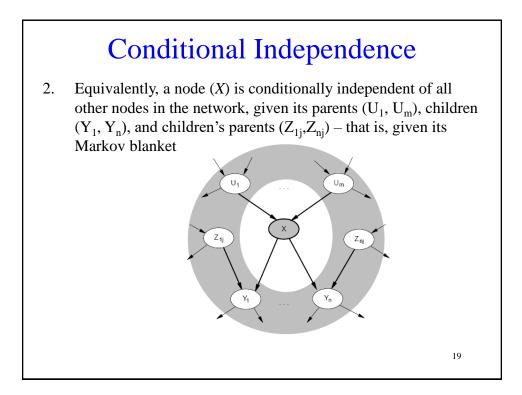
This is easy – we just label the nodes according to the partial order in the graph

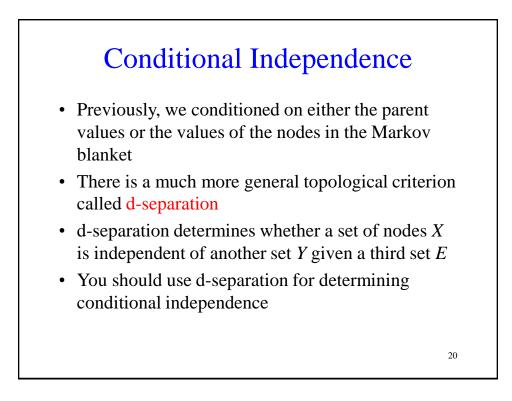
2. We need X_i to be conditionally independent of its predecessors given its parents

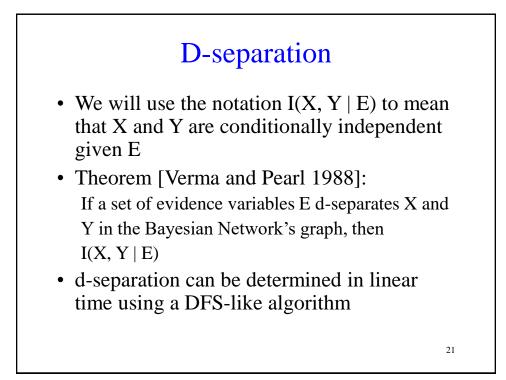
This can be done when constructing the network. Choose parents that directly influence X_i .

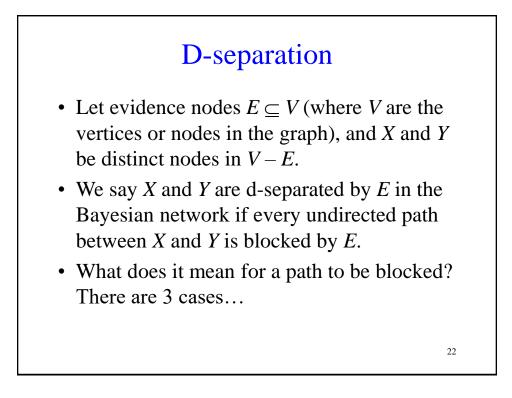


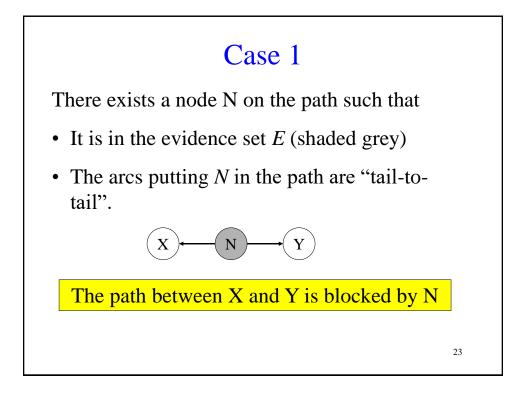


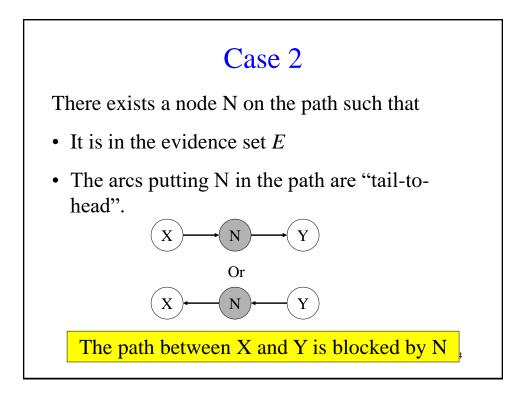


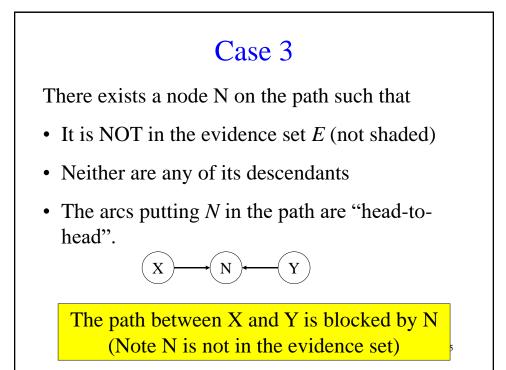


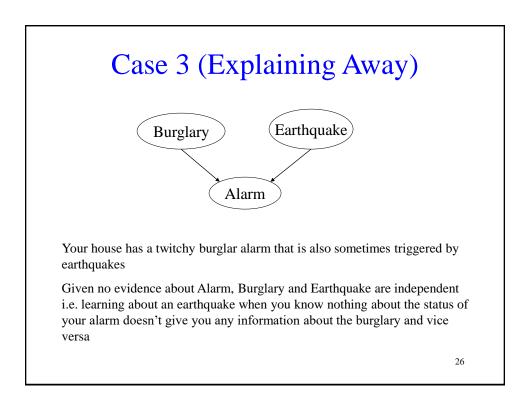


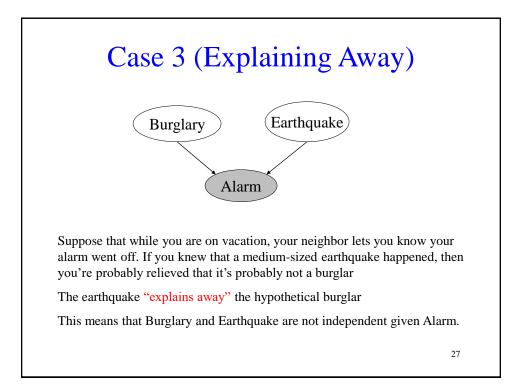


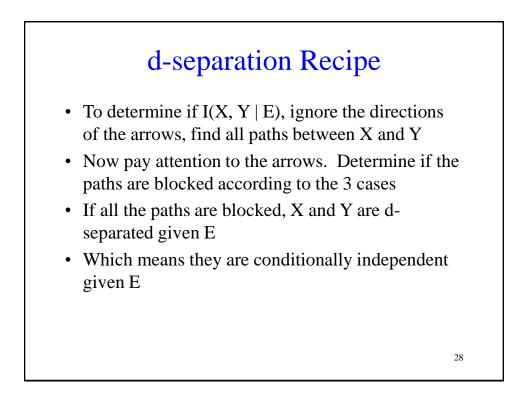


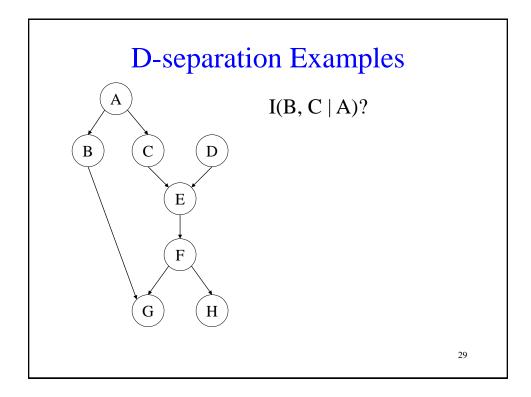


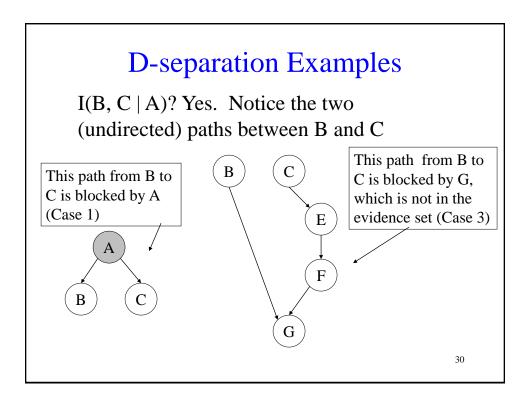


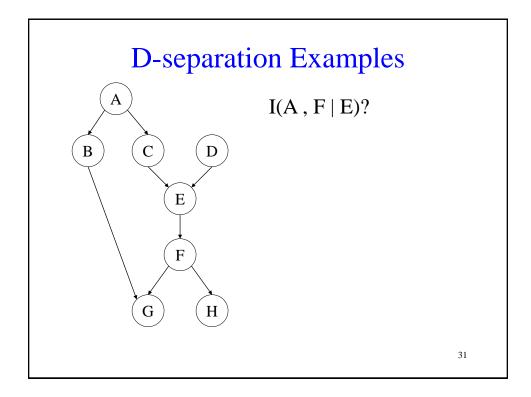


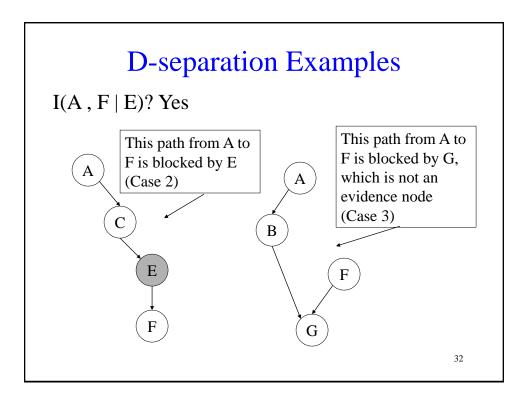


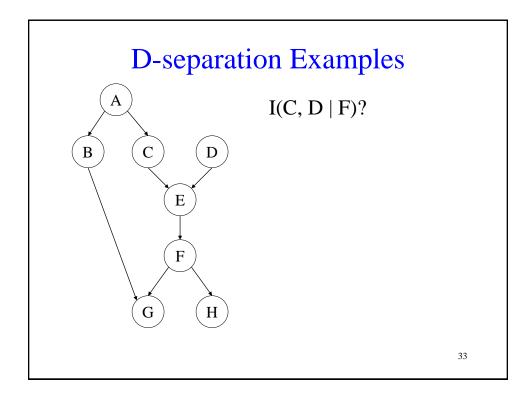


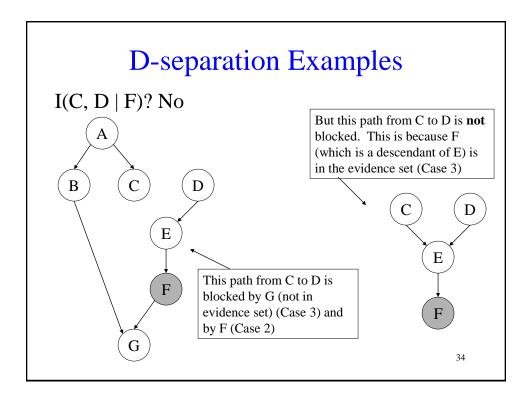


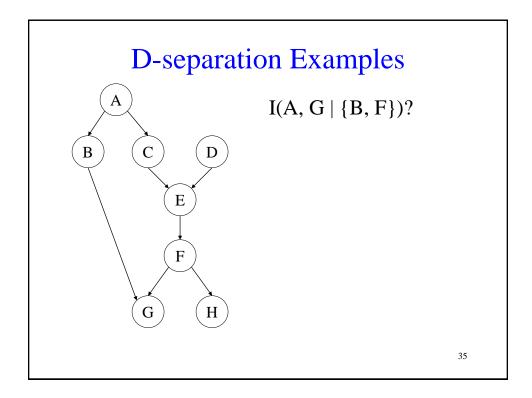


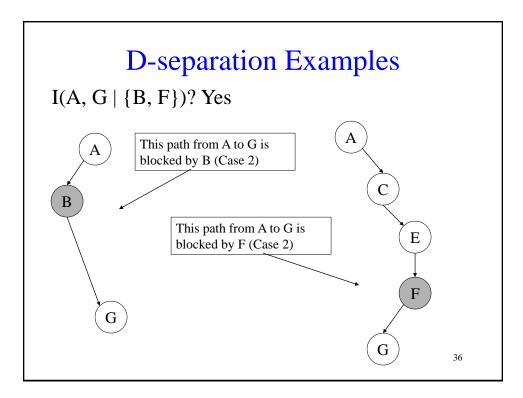


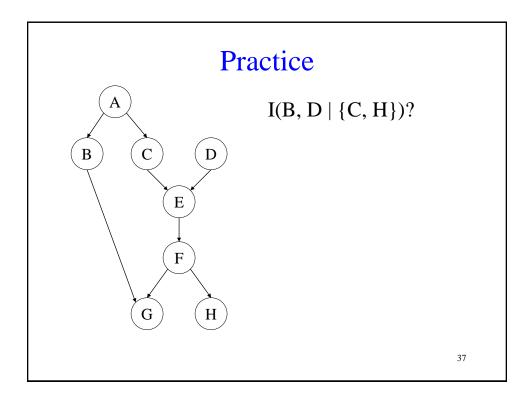


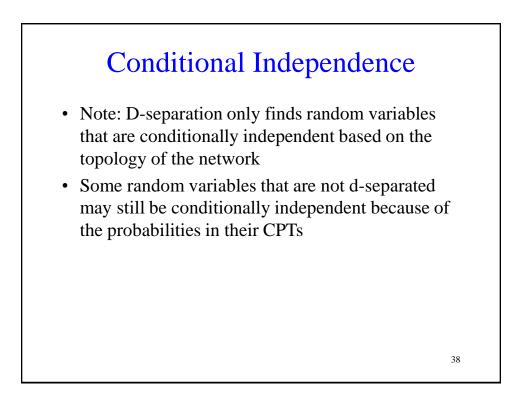












What You Should Know

- How to compute the joint probability distribution from a Bayesian network
- How to determine conditional independence relationships using d-separation