

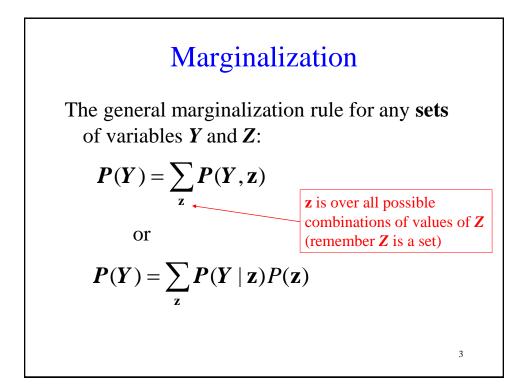
Thanks to Andrew Moore for some course material

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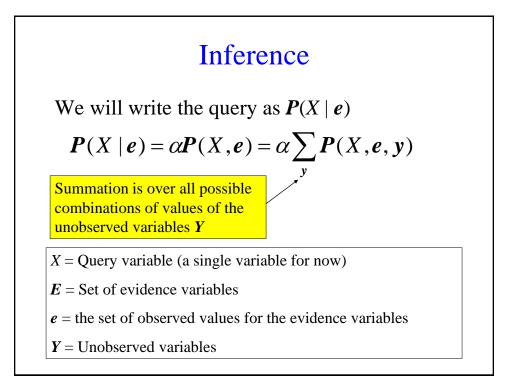
Fι	Full Joint Probability Distributions					
Coin	Card	Candy	P(Coin, Card, Candy)	7		
tails	black	1	0.15			
tails	black	2	0.06	The probabilities		
tails	black	3	0.09	in the last column		
tails	red	1	0.02	sum to 1		
	-					

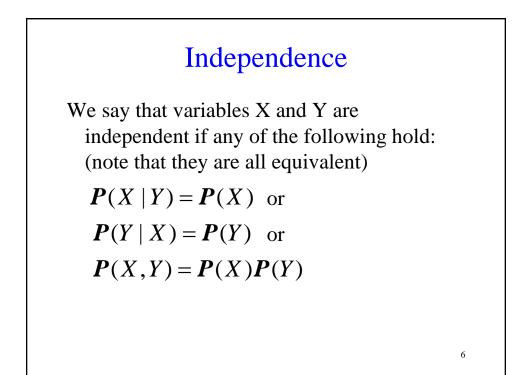
tails	red	1	0.02	sum to 1
tails	red	2	0.06	
tails	red	3	0.12	
heads	black	1	0.075	
heads	black	2	0.03	
heads	black	3	0.045	
heads	red	1	0.035	
heads	red	2	0.105	
heads	red	3	0.21	•

This cell means P(Coin=heads, Card=red, Candy=3) = 0.21



Conditional Probabilities We can also compute conditional probabilities from the joint. Recall: $P(A|B) = \frac{P(A,B)}{P(B)}$





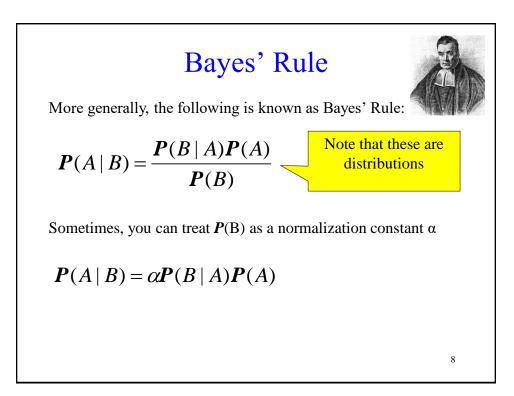


The product rule can be written in two ways: P(A, B) = P(A | B)P(B)P(A, B) = P(B | A)P(A)

You can combine the equations above to get:

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$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)}$$



More General Forms of Bayes Rule

If A takes 2 values:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|\neg A)P(\neg A)}$$

If A takes n_A values:

$$P(A = v_i | B) = \frac{P(B | A = v_i)P(A = v_i)}{\sum_{k=1}^{n_A} P(B | A = v_k)P(A = v_k)}$$

When is Bayes Rule Useful?

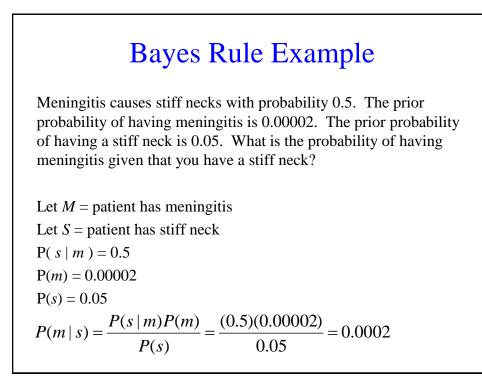
Sometimes it's easier to get P(X|Y) than P(Y|X).

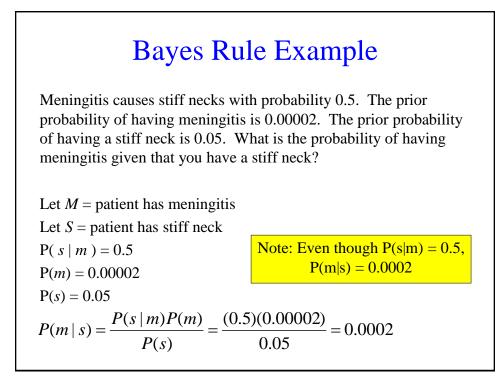
Information is typically available in the form P(effect | cause) rather than P(cause | effect)

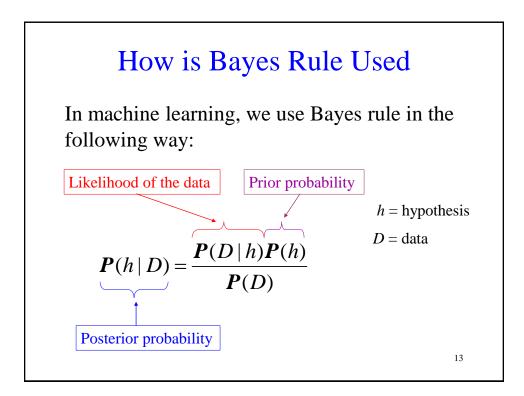
For example, P(symptom | disease) is easy to measure empirically but obtaining P(disease | symptom) is harder

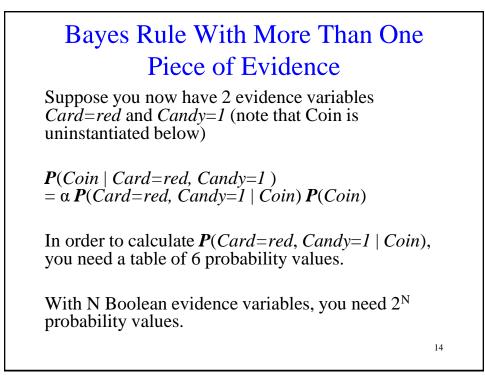
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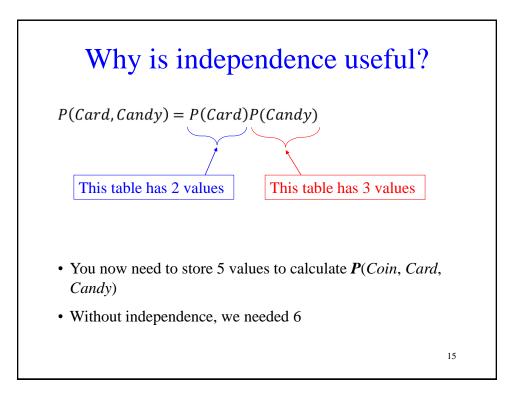
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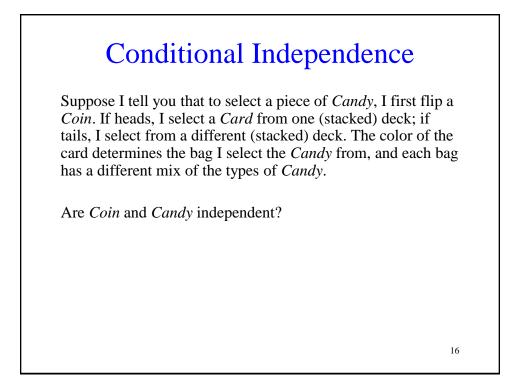


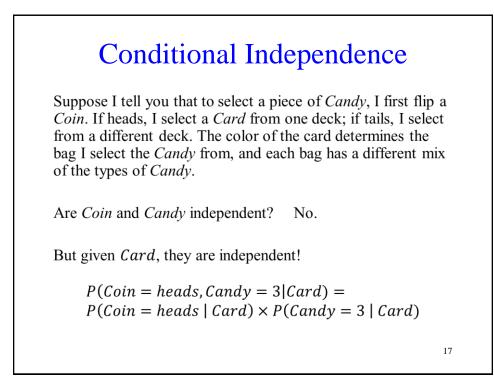


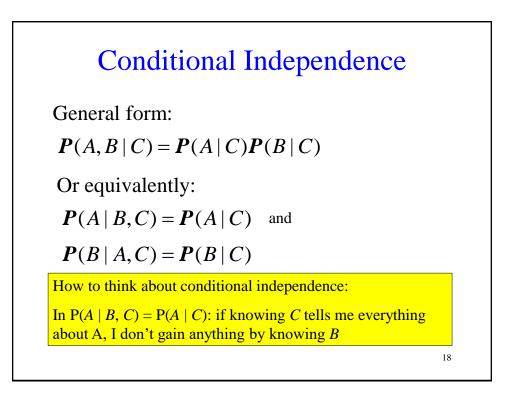


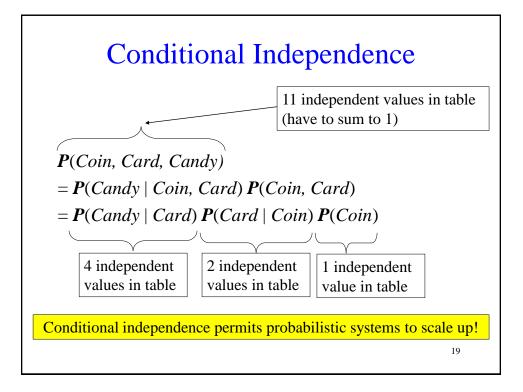












Coin	P(Coin)	Coin	Card	P(Card Coin)	Card	Candy	P(Candy Card)
tails	0.5	tails	black	0.6	black	1	0.5
heads	0.5	tails	red	0.4	black	2	0.2
		heads	black	0.3	black	3	0.3
		heads	red	0.7	red	1	0.1
					red	2	0.3
					red	3	0.6
	P(Coin	a = hec	ıds) >	ls, Card = re $< P(Card = red) = red) = red$		2	

