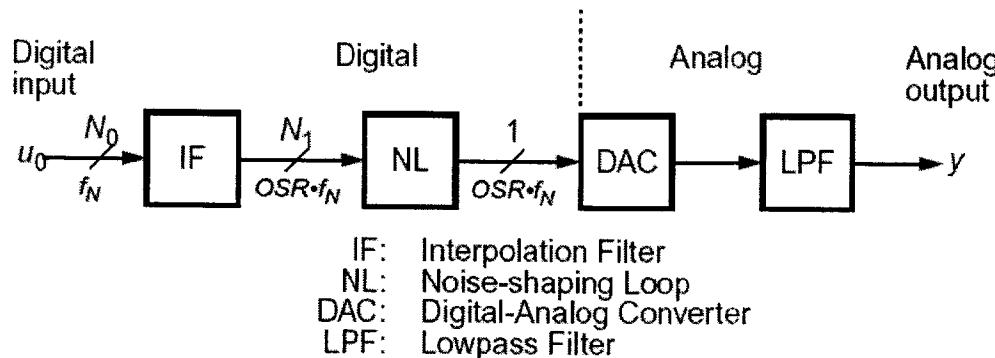
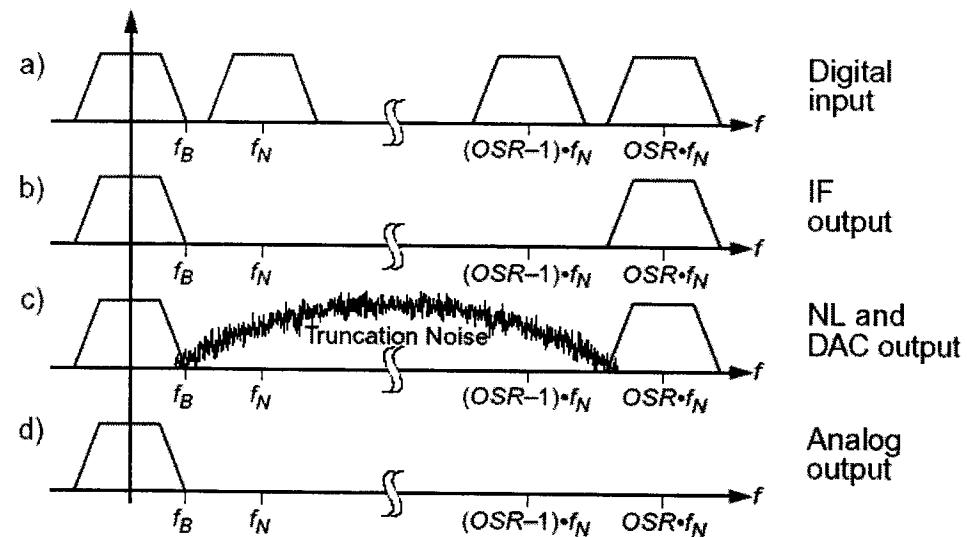


# $\Delta\Sigma$ DAC STRUCTURE



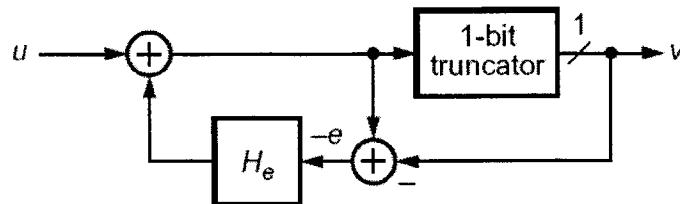
Block diagram of a  $\Delta\Sigma$  DAC.

**Single-bit DAC can be linear. For a few bits (2~4), DEM can be used**



Signal and noise spectra in a  $\Delta\Sigma$  DAC.

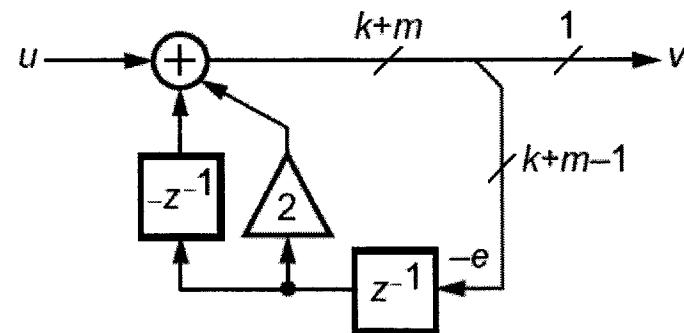
# ERROR FEEDBACK ARCHITECTURE



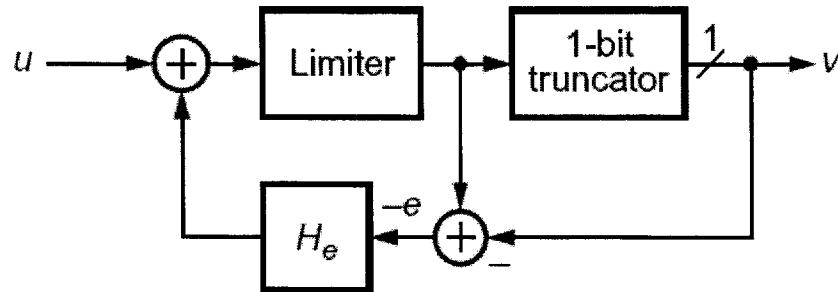
Error feedback structure.

$$V(z) = U(z) + [1 - H_e(z)]E(z)$$

$$H_e(z) = 1 - (1 - z^{-1})^2 = z^{-1}(2 - z^{-1})$$



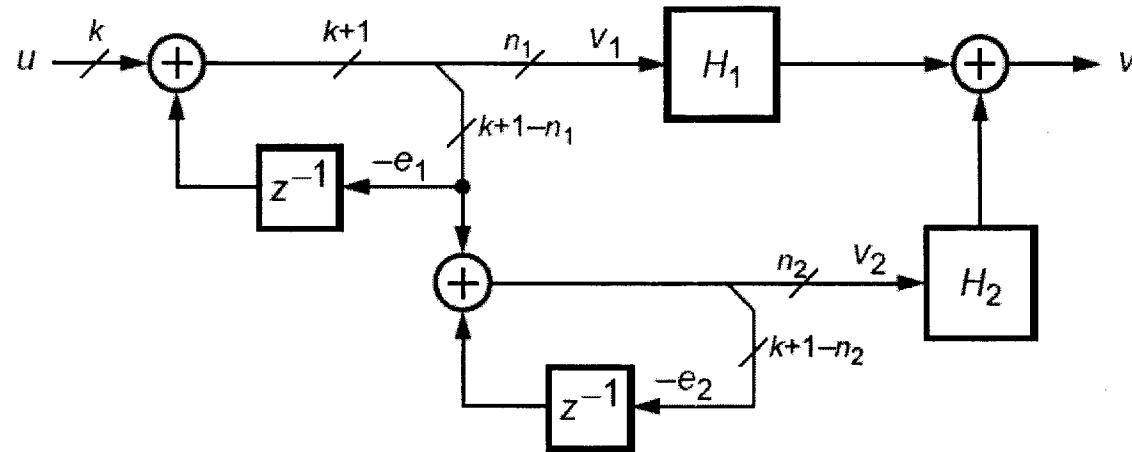
Second-order error-feedback noise-shaping loop.



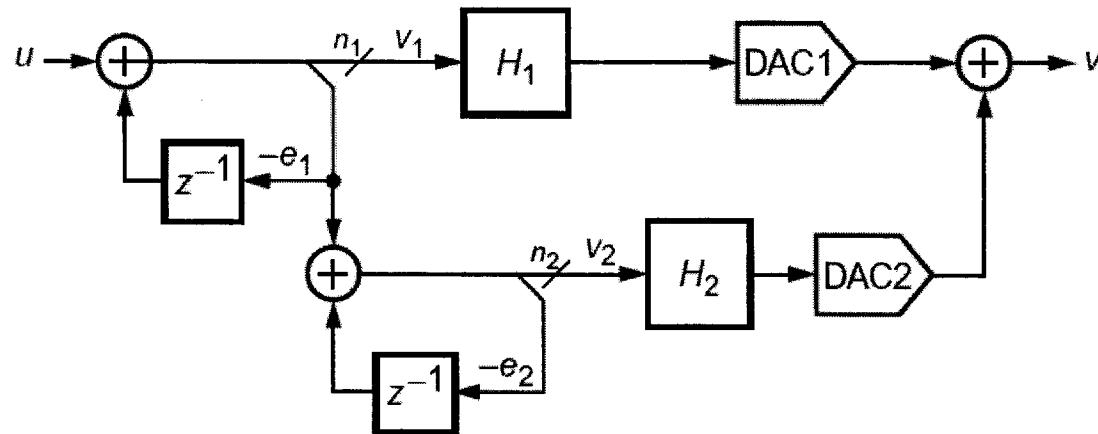
Error feedback with limiter.

Also, all  $\Delta\Sigma$  configurations can be used

# CASCADE DACs

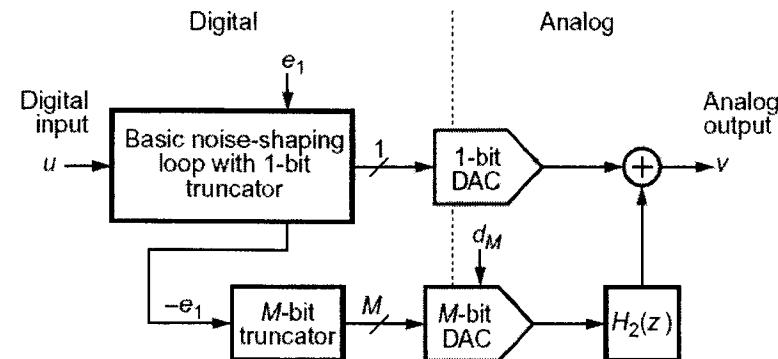


Cascade structure for a second-order noise-shaping loop.

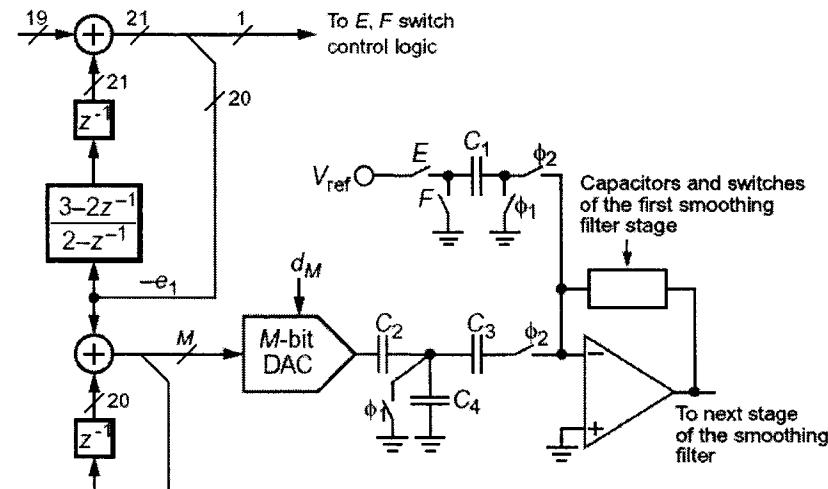


A cascade DAC using analog recombination.

# DUAL TRUNCATION DACs



A dual-truncation DAC system.

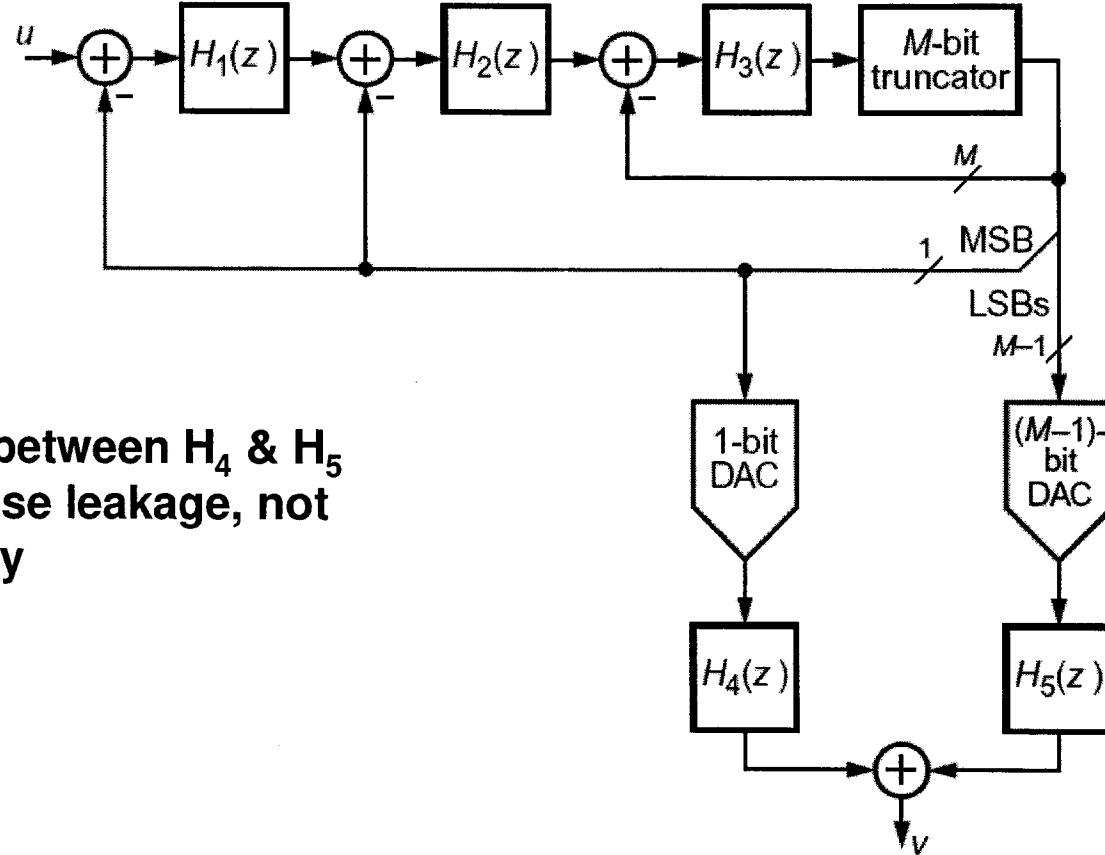


A third-order dual-truncation MASH noise-shaping stage.

A dual-truncation MASH structure.

# HARAPETIAN'S SCHEME

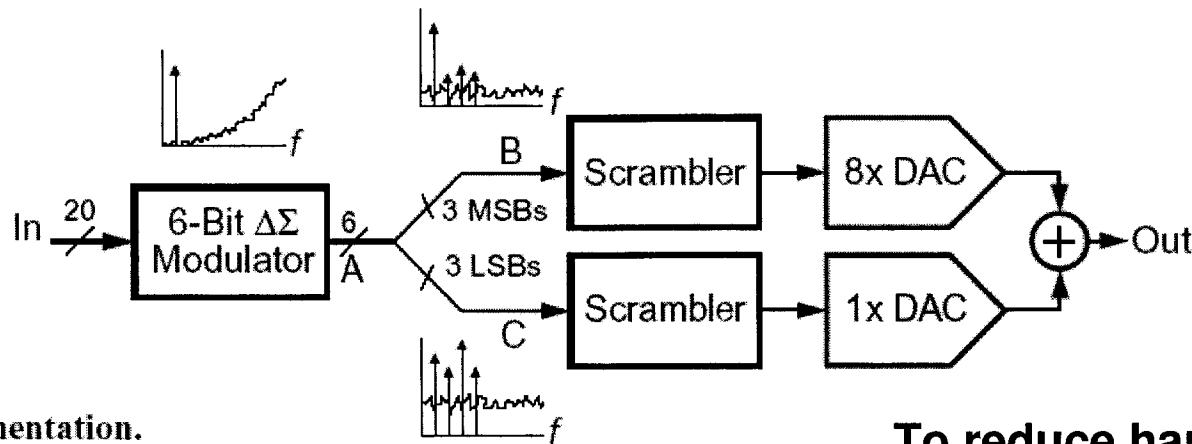
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**Mismatch between  $H_4$  &  $H_5$   
causes noise leakage, not  
nonlinearity**

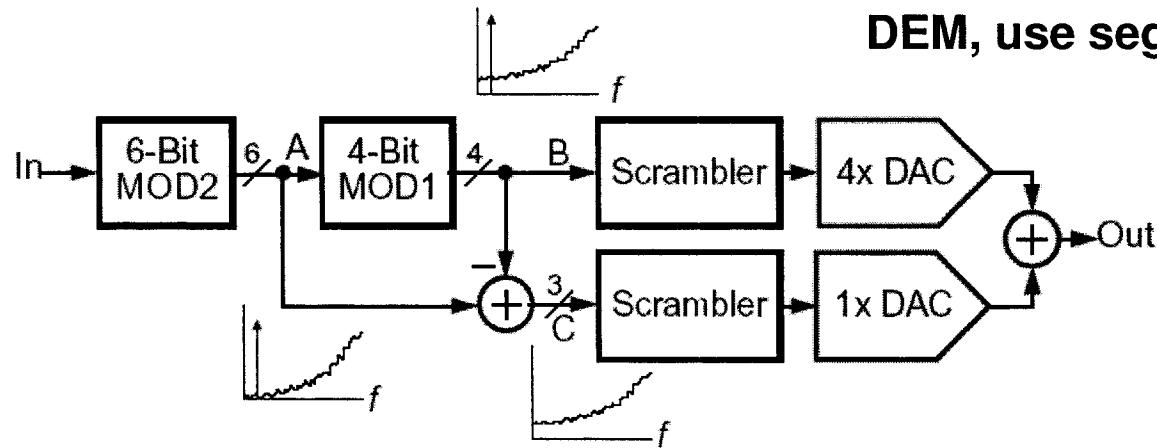
A single-stage dual-truncation D/A loop.

# SEGMENTED DACs



Segmentation.

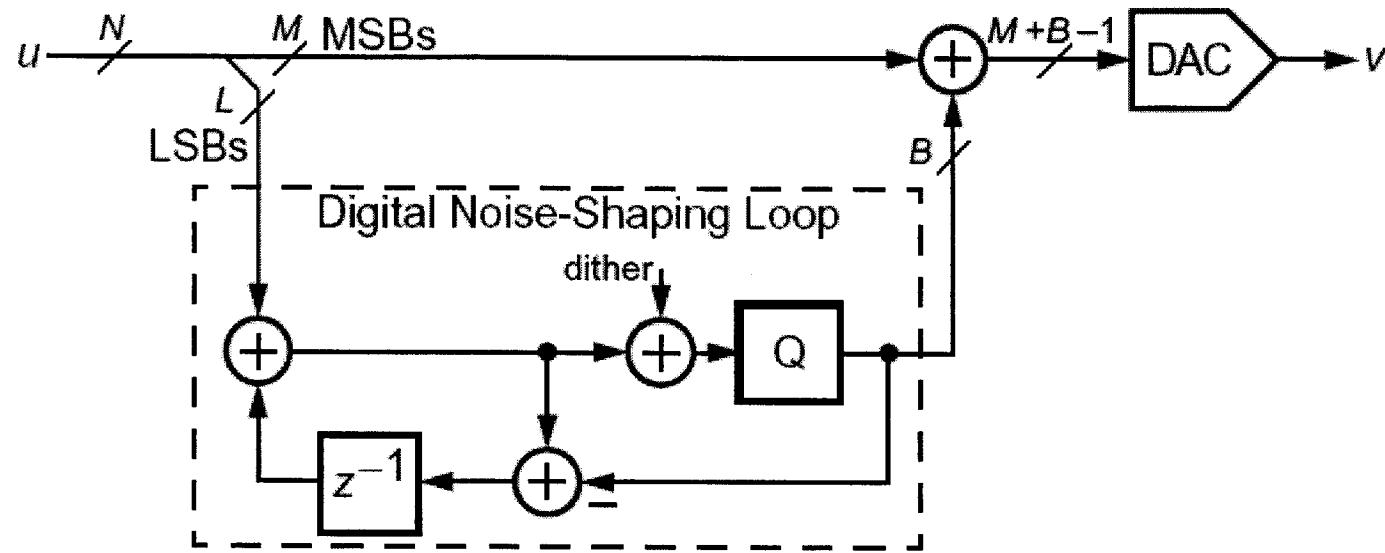
To reduce hardware  
needed in the DAC and the  
DEM, use segmentation



Noise-shaped segmentation.

# ANOTHER SEGMENTATION SCHEME

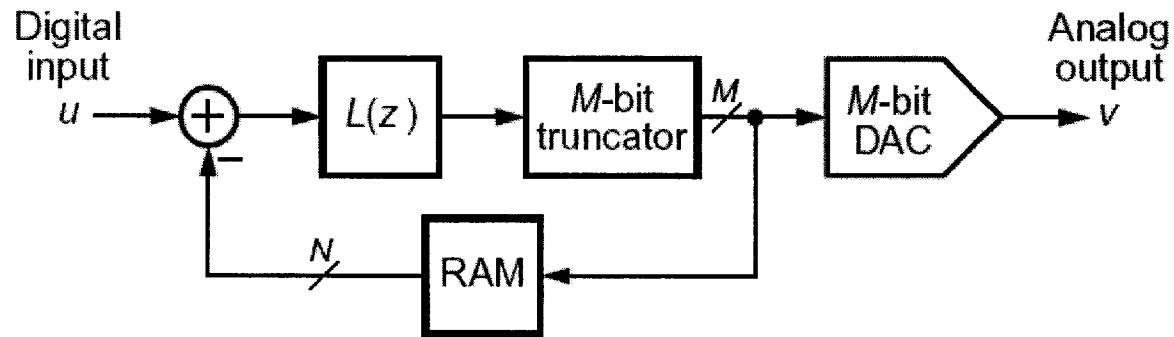
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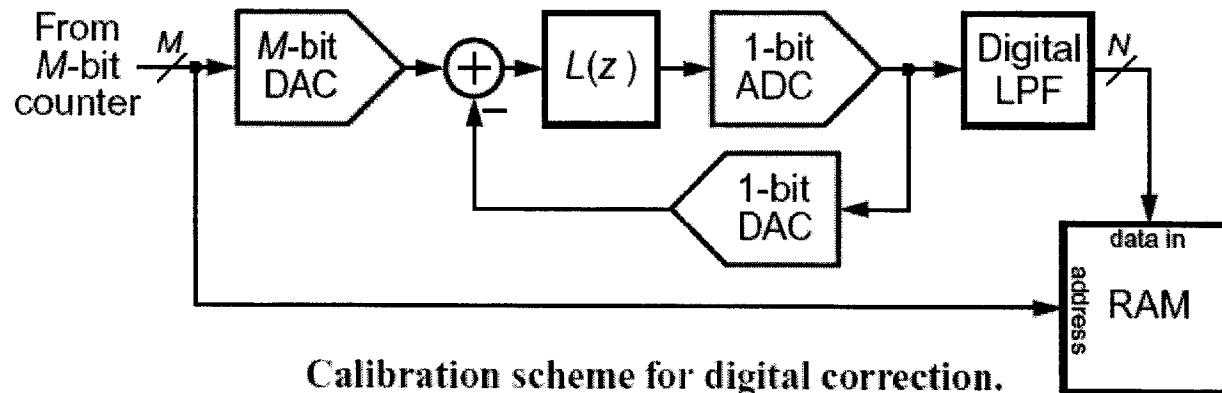
A hardware-reduced first-order modulator with dither.

# A POWER-UP CORRECTION METHOD

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A digitally-corrected  $M$ -bit DAC.



Calibration scheme for digital correction.

# COMPARISON OF SINGLE- AND MULTI-BIT $\Sigma\Delta$ DACS

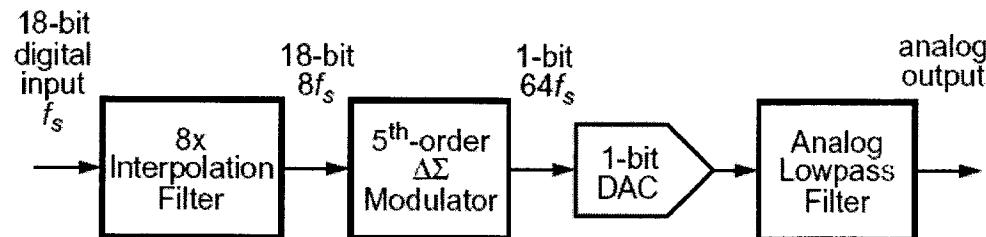
**Single-bit truncation:** Much simpler internal DAC structure can be used, without the need for thermometer coding, unit elements and digital mismatch-shaping logic.

**Multi-bit truncation:** Several advantages can be obtained, including

1. Simpler digital noise-shaping loop, since more aggressive NTF may be used, and since the truncation noise is reduced by at least  $N - 1$  bits.
2. Less (or no) dithering, since tones are less likely to be generated, and since typically the amplitude of dithering is about 1/2 LSB, which is smaller in a multi-bit quantizer.
3. Much simpler analog smoothing filter, since the slewing and out-of-band noise in the DAC output are both reduced. Also, the sensitivity to clock jitter is reduced, due to the reduced step size in the DAC output signal.<sup>†</sup>

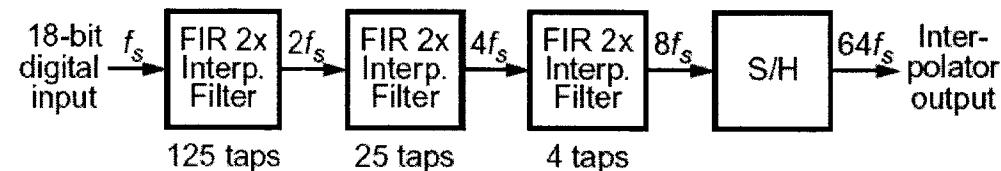
Generally, the advantages of multi-bit truncation outweigh those of single-bit truncation, and hence it is preferable to design  $\Delta\Sigma$  DACs with multi-bit internal DACs.

# AN EXAMPLE [3]

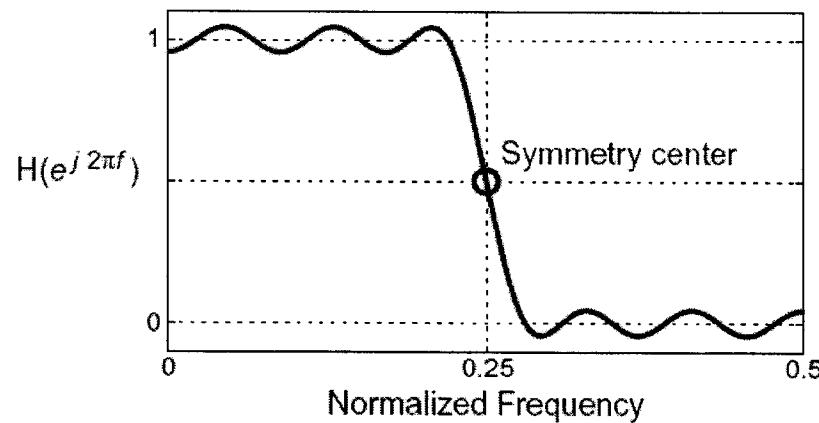


An 18-bit D/A converter architecture.

Interpolation filter architecture.

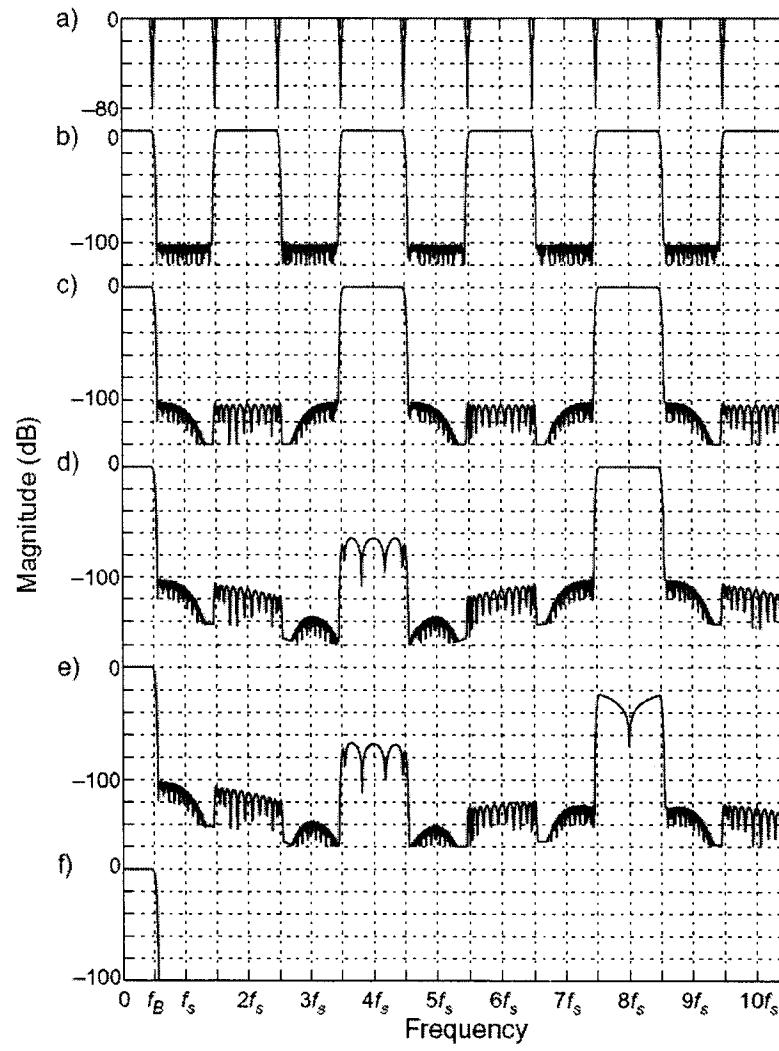


Frequency response of a half-band filter.

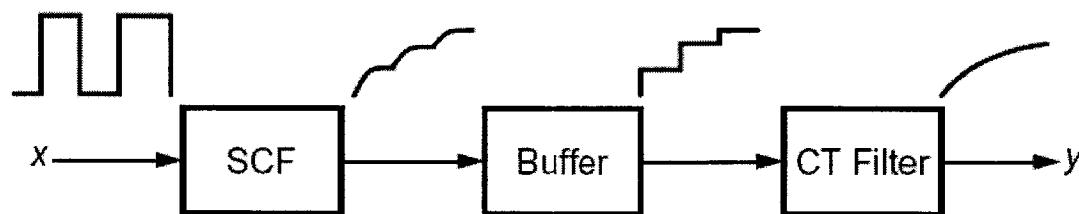


# SPECTRA WITHIN $\Delta\Sigma$ DAC SYSTEM

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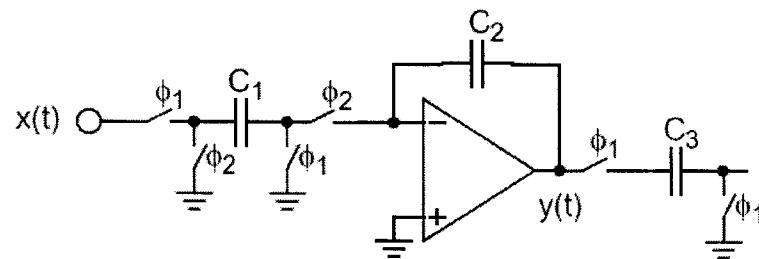


# POST-FILTER DESIGN

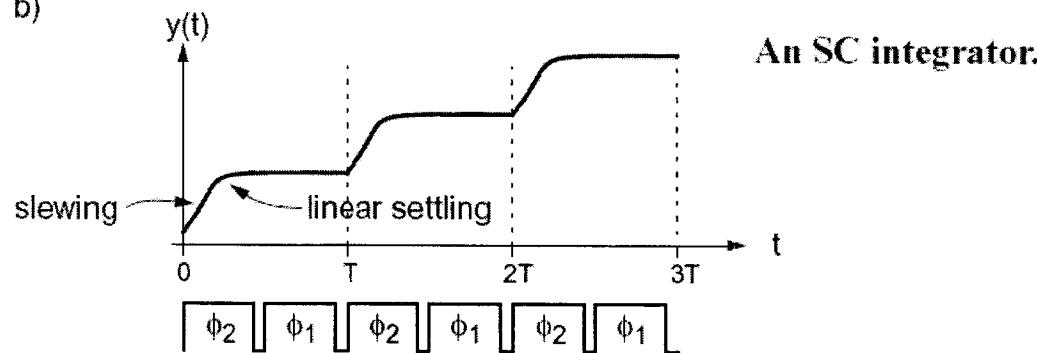


Post-filter for a 1-bit  $\Delta\Sigma$  DAC and associated signals.

a)

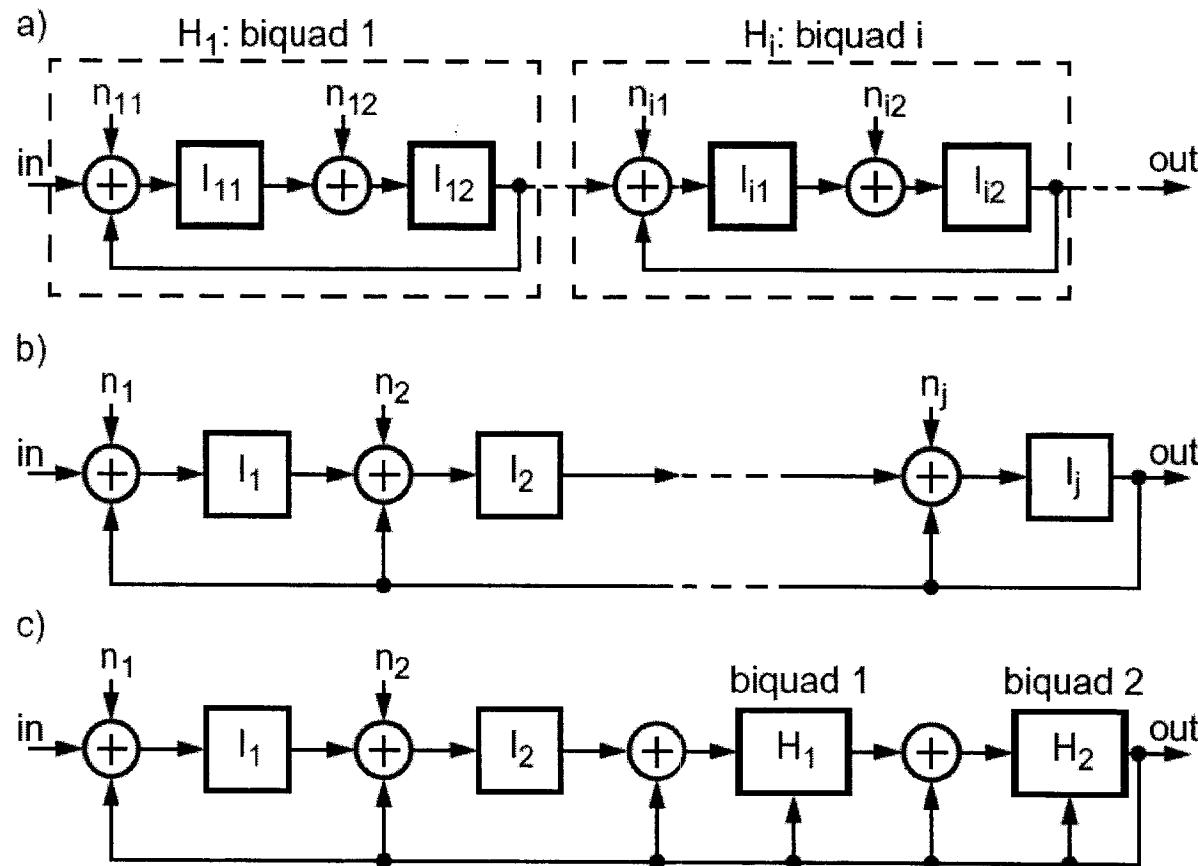


b)



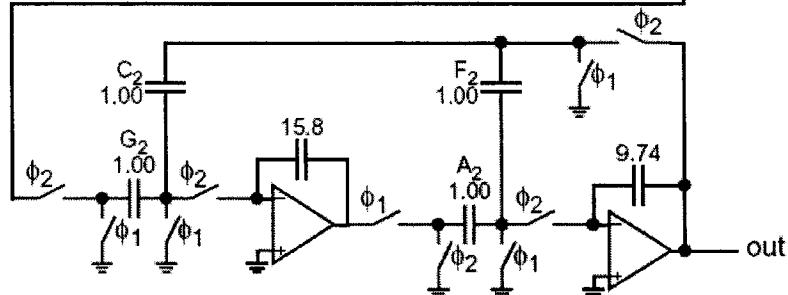
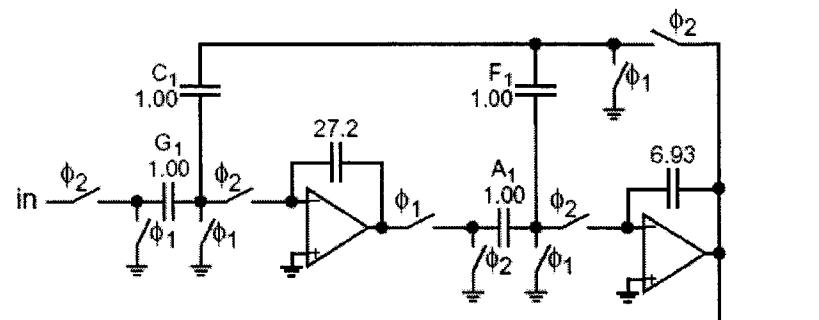
An SC integrator.

# RECONSTRUCTION FILTER ARCHITECTURES

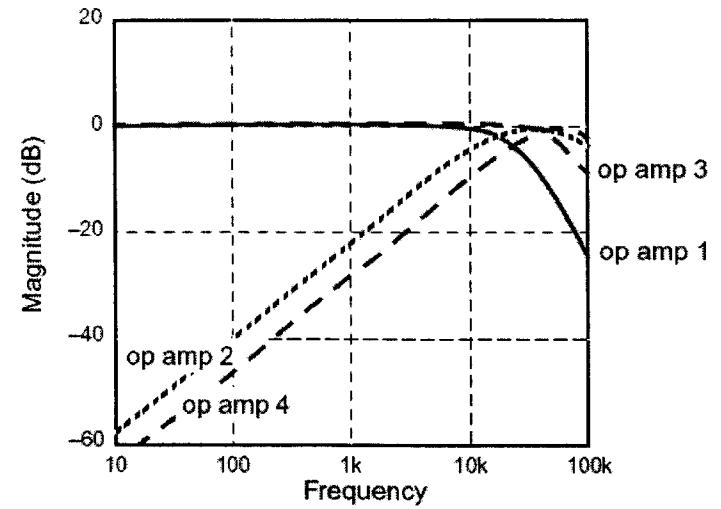


# POST-FILTER EXAMPLES (1)

A 4<sup>th</sup>-order Bessel filter implemented with a cascade of biquads.

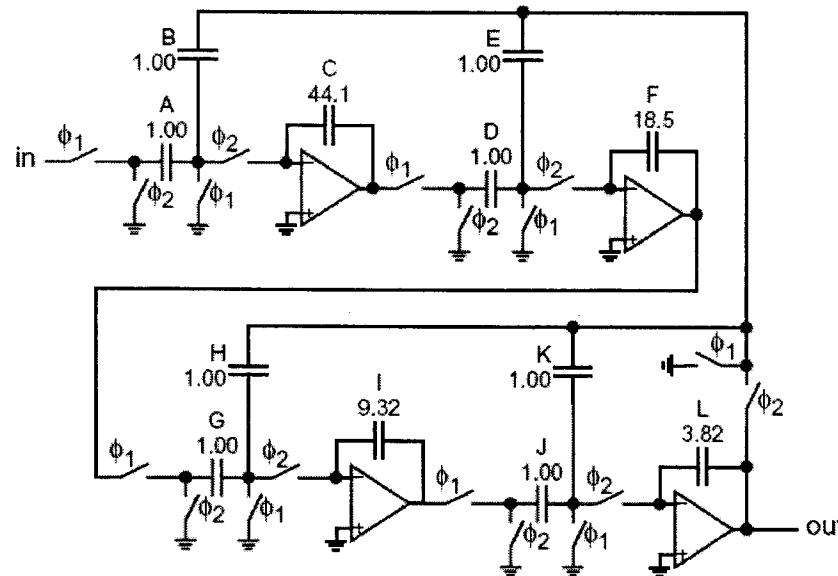


Noise gains from each op-amp input

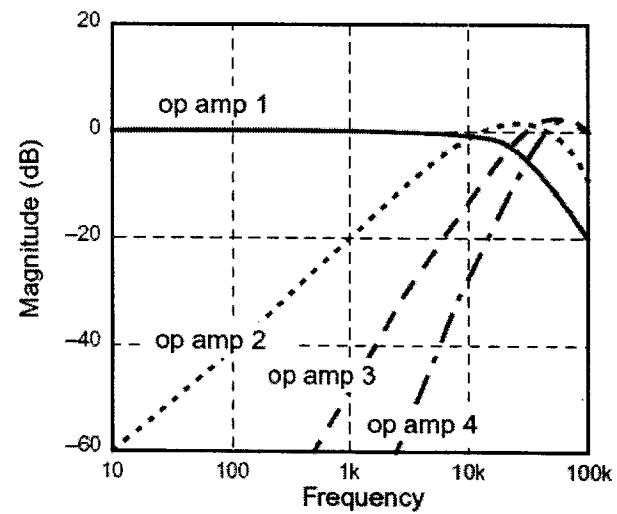


# POST-FILTER EXAMPLES (2)

A 4<sup>th</sup>-order Bessel filter implemented with the inverse follow-the-leader topology.

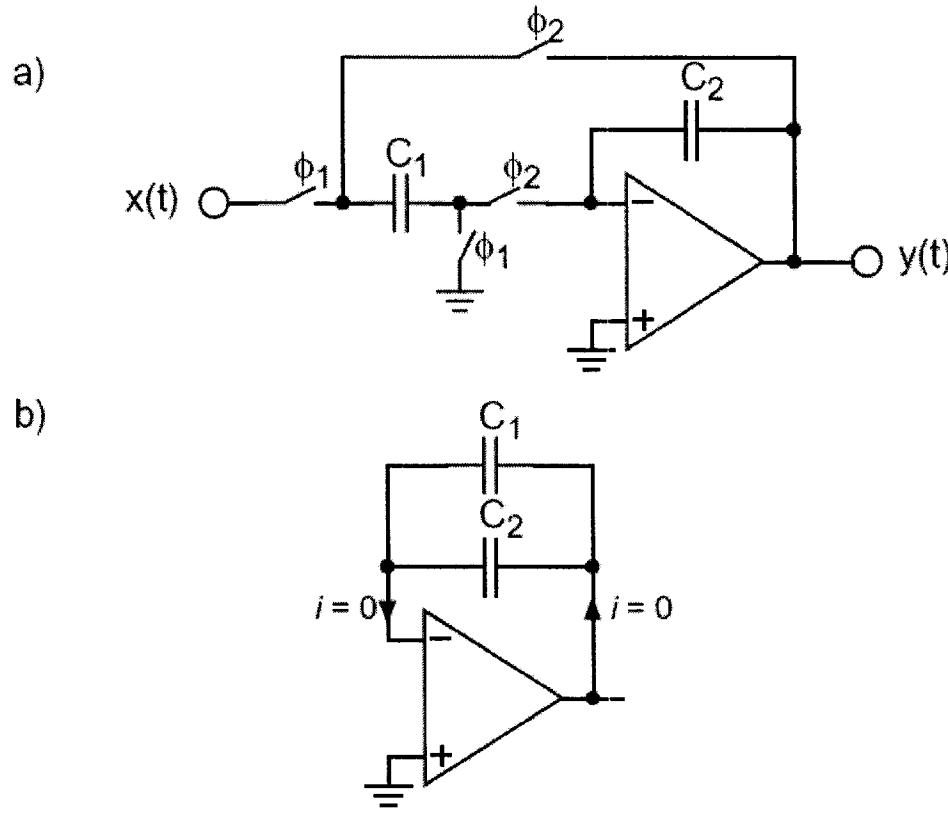


Noise gains from each op-amp input



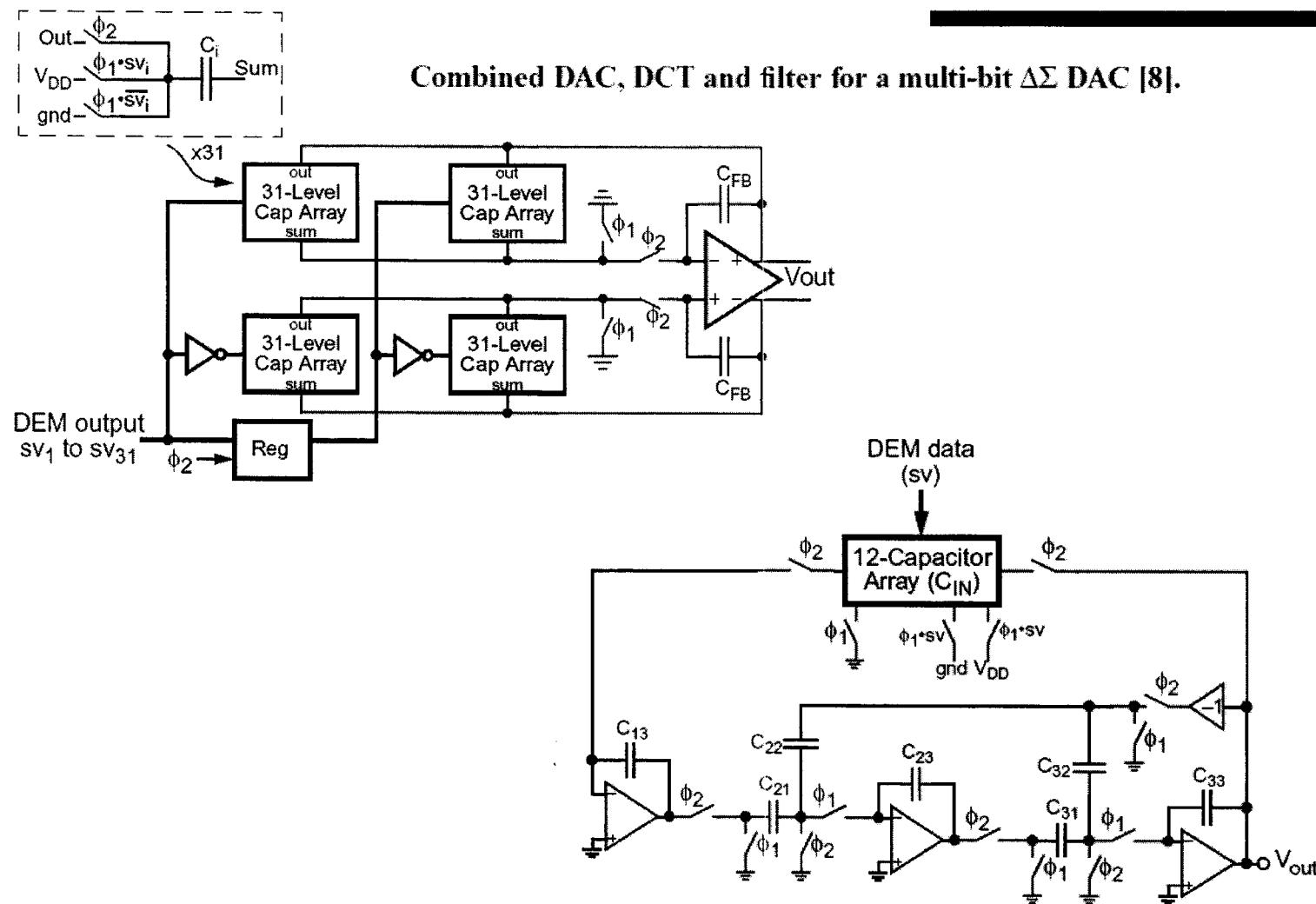
# SC-CT BUFFER

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A direct-charge-transfer (DCT) stage.

# DESIGN EXAMPLES



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- [13] J.A.C. Bingham, "Applications of a direct-transfer SC integrator," *IEEE Transactions on Circuits and Systems*, vol. 31, pp. 419-420, Apr 1984.
- [14] See, e.g., R. Schaumann and M.E. Van Valkenburg, *Design of Analog Filters*, pp. 161-163, Oxford University Press, 2001.
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